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## Medians

In  $\triangle ABC$ , let M, N, and P be midpoints of AB, BC, AC.

Medians: CM, AN, BP

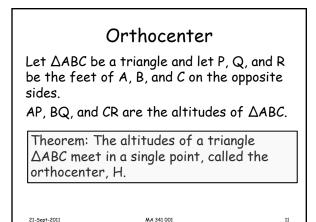
Theorem: In any triangle the three medians meet in a single point, called the centroid.

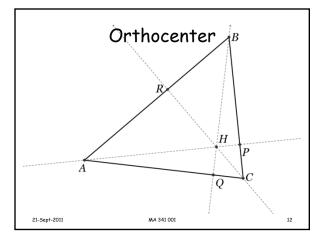
M - midpoint  $\Rightarrow$  AM=BM, N - midpoint  $\Rightarrow$  BN=CN P - midpoint  $\Rightarrow$  AP=CP

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 $\overline{MB} \cdot \overline{NC} \cdot \overline{PA} = 1$ 

By Ceva's Theorem they are concurrent. 21-Sept-2011 MA 341 001







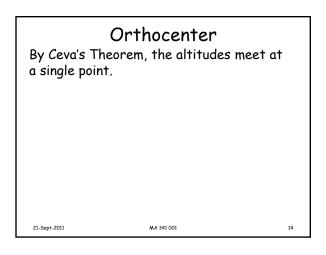
## Orthocenter

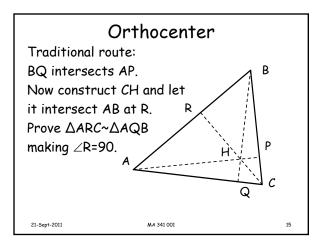
By AA

 $\Delta BRC \sim \Delta BPA \text{ (a right angle and } \angle B\text{)}$   $\Rightarrow BR/BP=BC/BA$   $\Delta AQB \sim \Delta ARC \text{ (a right angle and } \angle A\text{)}$   $\Rightarrow AQ/AR=AB/AC$   $\Delta CPA \sim \Delta CQB \text{ (a right angle and } \angle C\text{)}$   $\Rightarrow CP/CQ=AC/BC$   $\frac{BR}{BP} \cdot \frac{AQ}{AR} \cdot \frac{CP}{CQ} = \frac{BC}{AB} \cdot \frac{AB}{AC} \cdot \frac{AC}{BC} = 1$ 21-Sept-2011
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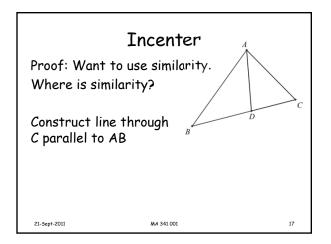


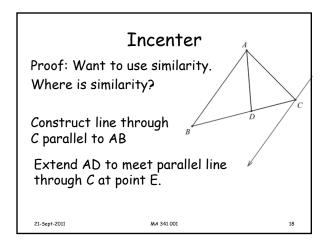


	Incenter	
	a triangle and let . angle bisectors o	
Angle Bisector Theorem: If AD is the angle bisector of $\angle A$ with D on BC, then $\frac{AB}{AC} = \frac{BD}{CD}$		
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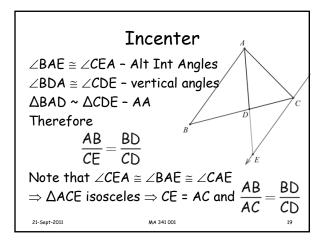
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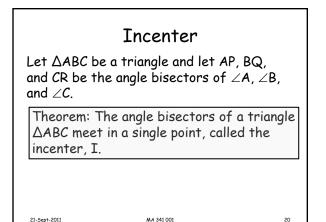


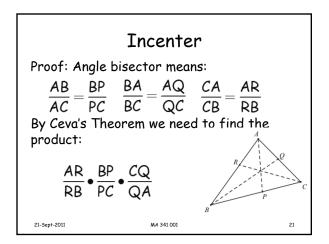




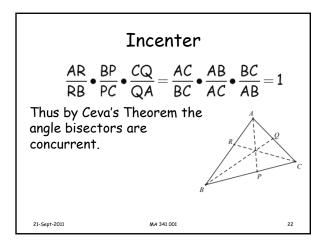




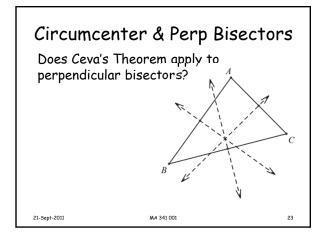




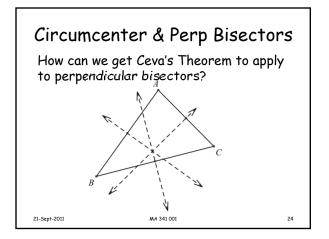




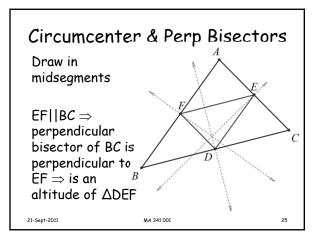




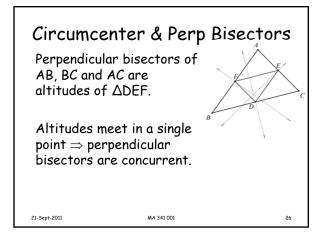






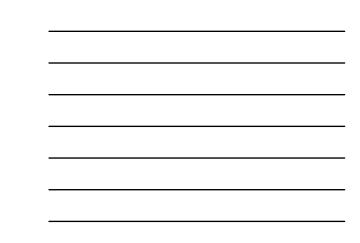


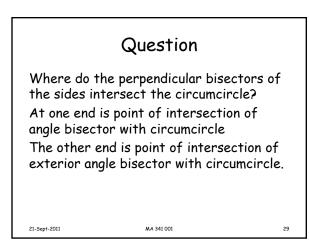


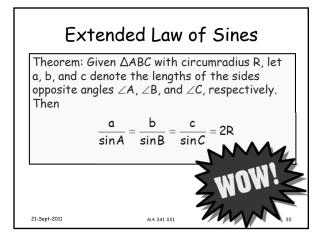


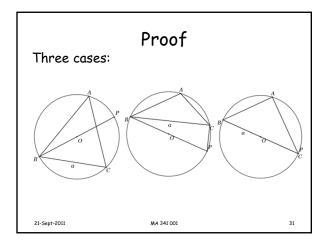
Theorem: Th any three no	here is exactly one circle through on-collinear points.
The center :	the circumcircle = the circumcenter, O. = the circumradius, R.

Question	
Where do the perpendicular bisectors of the sides intersect the circumcircle?	
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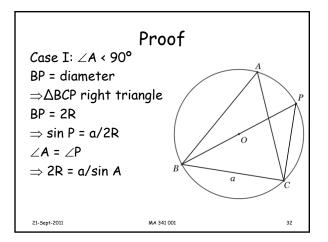




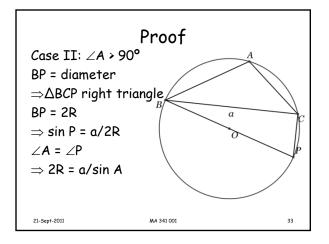


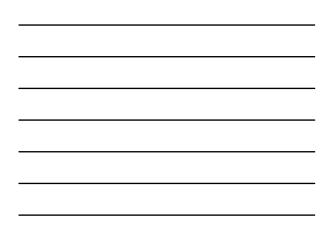


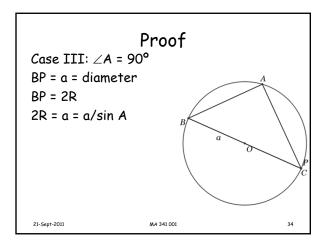




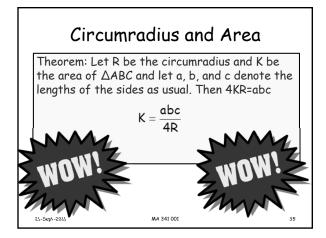














Proof	
K = $\frac{1}{2}$ ab sin C 2K = ab sin C c/sin C = 2R sin C = c/2R 2K = abc/2R 4KR = abc	
4KR = abc	

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