MA 341 — Homework #1

Due Friday, September 5, in class

We saw in class that an equation of a line containing the distinct points (x_1, y_1) and (x_2, y_2) is given by

$$(y_1 - y_2)x + (x_2 - x_1)y = x_2y_1 - x_1y_2.$$

Knowing this, now assume that (x_1, y_1) , (x_2, y_2) , and (x_3, y_3) are three distinct points and consider the expression

$$A = x_1 y_2 + x_2 y_3 + x_3 y_1 - x_1 y_3 - x_2 y_1 - x_3 y_2$$

- 1. Prove that if the three points all lie on a common line then A = 0.
- 2. Conversely, prove that if A = 0 then the three points all lie on a common line.
- 3. Do a lot of experiments with actual points to try to figure out what geometric meaning the quantity A has. That is to say, if you plot the three points, make a good guess backed by your evidence as to what A measuring. It is not necessary (yet) to prove your conjecture.