MA515 HOMEWORK #5 Due Wednesday, October 3

- 1. Exercise 7.28
- 2. Exercise 7.29
- 3. Exercise 7.34
- 4. Let us assume we have an LP of the form

$$\max z = c^T x$$

s.t. $Ax = b$
 $x \ge O$

- (a) Let \overline{x} be a feasible point. Prove that \overline{x} is a basic feasible solution if and only if it is a vertex (using our earlier definition of vertex involving $N(\overline{x})$).
- (b) Assume that we have a basic feasible solution \overline{x} associated with some basis B, and that we also have some basic direction \overline{w} associated with B and nonbasic $s \in N$. For convenience, let us also assume that $\overline{x}_j > 0$ for each $j \in B$ and that \overline{w} is not nonnegative. So when we consider the ray $\overline{x} + t\overline{w}, t \ge 0$, we will discover some leaving variable $x_r, r \in B$. Prove that $B' = (B \cup \{s\}) \setminus \{r\}$ is a basis; i.e., prove that the columns of $A_{B'}$ are linearly independent.