# STA 291 Lecture 29 

## - Review

## Final Exam, Thursday, May 6

- When: 6:00pm-8:00pm
- Where: cв 106

Make-up exam: Friday 10:00am-12:00noon

- Only by prior arrangement
- Room still unknown, watch the web for update, or come to $8^{\text {th }}$ floor POT on Friday
- Update: Makeup room: CB 303


## Final Exam, Thursday, May 6

- It will be approx. one and half length long compared to the two midterms. (i.e. if midterm have 20 questions, final will have approx. 30 questions).
- Similar mixture of open answer questions and multiple choice questions, compared to the midterms.
- Covers all the topics (comprehensive). But more on the later (testing hypothesis, confidence interval) materials.
- Formula sheet and tables will be provided.


## Some topics we covered

- Testing hypothesis.
- Confidence intervals. (even though it had been covered in midterm exam II)
- Connection between the above 2 topic.
- Use of Z (Normal) table to find probability
- When to use t-table instead?
- Setting up the correct hypothesis: -- it is always about a population parameter(s)
- Find the correct formula for the hypothesis
- Computation of the test statistic, and the P -value (Need to use table)
- What to do if falls outside the range of table?
- Reach a conclusion by compare the P value to the alpha level. ( report the Pvalue)
- Potential error (which type?)


## Connection between testing hypothesis and confidence interval

- Given a confidence interval, you can tell if the P -value is above or below alpha
- Given a P-value you can tell if the confidence interval will contain mu0
- Similar question on Exam II might reappear on final.


## Comparing paired Samples: Example

| Student | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Before | 60 | 73 | 42 | 88 | 66 | 77 | 90 | 63 | 55 | 96 |
| After | 70 | 80 | 40 | 94 | 79 | 86 | 93 | 71 | 70 | 97 |

a) Compare the mean weights after and before the drug by
i. finding the difference of the sample means
ii. finding the mean of the difference scores. Compare. ---(same)
iii. But SD is different, One SD or two SD's?
b) Calculate and interpret the P-value for testing whether the mean change equals 0
c) Compare the mean weights after and before taking the drug by constructing and interpreting a 90\% confidence interval for the population mean difference

## Comparing Dependent Samples: Example (contd.)

## Output from Statistical Software Package SAS

| N | 10 |
| :--- | ---: |
| Mean | 7 |
| Std Deviation | 5.24933858 |

$$
\text { Tests for Location: } \mathrm{Mu} 0=0
$$

| Test | -Statistic- |  | -----p Value------ |  |
| :---: | :---: | :---: | :---: | :---: |
| Student's t | t | 4.216901 | $\operatorname{Pr}>\|t\|$ | 0.0022 |
| Sign | M | 4 | $\operatorname{Pr}>=\|\mathrm{M}\|$ | 0.0215 |
| Signed Rank | S | 25.5 | $\operatorname{Pr}>=\|S\|$ | 0.0059 |

## Which method to chose?

- Two-year Italian study on the effect of condoms and the spread of AIDS
- Heterosexual couples where one partner was infected with HIV virus
- 171 couples who always used condoms: 3 partners became infected with HIV
- 55 couples who did not always use condoms: 8 partners became infected with HIV
- Test whether the rates are significantly different. Report the $P$-value and interpret.


## Which Method to Choose?

- A study compares the mean level of contributions to political campaigns in Pennsylvania by registered Democrats, and registered Republicans.


## Which Method to Choose?

- Example: Compare new drug to placebo in a double-blind clinical trial
- 24 patients
- Randomly pick 12 assign to placebo
- The other 12 receive the new drug
- Research question: Is there a different effect of placebo and new drug on a "response" on, for example, cholesterol, blood parameter, health status, weight,...


## Which Method to Choose?

- Example: Which of two suntan lotions (labeled $X$ and $Y$ ) provides better protection against sunburn
- 8 subjects expose their backs to the sun for a certain time, protected by suntan lotion
- Possible design:
- Randomly pick 4 subjects use lotion $X$
- the other 4 subjects use lotion Y


## Which Method to Choose?

- Example: Which of two suntan lotions (labeled $X$ and $Y$ ) provides better protection against sunburn
- 8 subjects expose their backs to the sun for a certain time, protected by suntan lotion
- Different design:
- Each of the 8 subjects uses both suntan lotions at the same time
- one lotion on the left side of the back, the other on the right side (use a coin flip to decide which side for X)


## Multiple Choice Question

- Which of the following statements are true?
" $95 \%$ confidence" means that
- $\quad 95 \%$ of the true population parameters are in the confidence interval
- If we were to repeat the procedure of sampling and calculating confidence intervals from the same population, then $95 \%$ of the population parameters are going to be in every calculated interval
- If we were to repeat the procedure of sampling and calculating confidence intervals from the same population, then $95 \%$ of the times our confidence interval will contain the true population parameter


## Multiple choice Q

- If a test turns out to be significant at alphalevel 0.01. (what exactly this mean for the p-value?)
- Will the same test also be significant at 0.05 level?
- P-value is NOT the probability that the H 0 is true.
- A small p-value mean that we saw something happened that is hard to explain by H0
- A large p-value do not automatically means H0 is true. (2 possibilities: either HO is true or there is too few data/info)
- Another H0 could have even larger Pvalue


## Test vs. Confidence Interval

Assume that the $p$-value is equal to 0.043 for a test of the null hypothesis $\mathrm{HO}: \mathrm{mu}=2$, with two-sided alternative.

What conclusion can we make about a $95 \%$ confidence interval for mu?

- Study hard and good luck!

