

Abstract /mathematical but necessary because this is the mathematical theory underlying all statistical inference

- Fundamental concepts that are very important to understanding Sampling Distribution, Confidence Interval, and P-Value
- Our goal is to learn the rules involved with assigning probabilities to events, and related calculations after assign probability.

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Probability: Basic Terminology

- Events: -- where probability live. usually denoted by A, B, C, etc. (We say probability of event A etc)
- Sample space is the largest event. S
- Sample Space: The collection of all possible outcomes of an experiment.

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- Event: A specific collection of outcomes.
- Simple Event: An event consisting of exactly one outcome.
- Each event is given (assign) a probability: a number between 0 and 1, inclusive. Denoted by P(A)

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 Could assign probability using a table (if we can list all events with their probabilities)

Otherwise, (with too many events) we need a rule of assign probability

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Sample Spaces, and Events Examples of experiment/sample space: 1. Flip a coin: {head, tail} 2. Flip a coin 3 times: {HHH, HHT, ...TTT} 3. Roll a die: {1,2,3,4,5,6} 4. Draw and record opinion of a SRS of size 50 from a population 5. Time your commuting time in a weekday morning. 6. Score of A football game between two chosen teams 7. Give AIDS patient a treatment and record how long he/she lives.

- There are often more than one way to assign probability to a sample space. (could be infinitely many ways)
- Statistical techniques we will learn later help identify which one "reflecting the truth".
- In Chap. 5 here we do not identify which probability is more "true" but just learn the consequences of a (legitimate) probability assignment.

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legitimate probability

- P(A) has to be a number between 0 and 1, inclusive (rule 1)
- The probability of the sample space S must be 1: P(S) =1 (rule 2)
- When we are able to list all simple events,
- O_i The summation over i for $P(O_i)$ must be 1

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$\Sigma P(O_i) = 1$

P(A) could be computed by sum of $P(O_i)$ over those O's inside A.

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Assigning Probabilities to Events

Example:

- - equally likely outcomes (classical approach)
- - relative frequency (using historical data)
- -- Subjective
- Monty Hall show: chance of winning is 1/3 or 1/2 ?

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• Both are legitimate, but only one is true.

Equally Likely Approach

- The equally likely outcomes approach usually relies on symmetry/geometry to assign probabilities to events.
- Suppose that an experiment has only n (distinct) outcomes. The equally likely approach to probability assigns a probability of 1/n to each of the outcomes.
- Further, if an event A is made up of m simple outcomes, then Prob(A) = P(A) = m/n.

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Notice the notation: event is denoted by capital letter A

- The probability assigned to this event is denoted by P(A) or Pr(A) or Prob(A)
- We say P(win) = 0.5 or P(win) = 0.65 etc.

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Assign Probability: Equally Likely
Approach
Examples:
1. Roll a fair die, the sample space is
{ 1, 2, 3, 4, 5, 6 }
There are 6 outcomes in sample space, each one
get a probability of 1/6.
 The probability of getting "5" is 1/6.
The probability of getting {"3" or above} is 4/6.
This does not mean that whenever you roll the die 6
times, you definitely get exactly one "5"

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• Flip a fair coin twice: sample space = $\{ (H, H), (H, T), (T, H), (T, T) \}$ There are four pairs. Each one gets ¼ probability. Let A = { two heads }, P(A) = ¼ Let A = {at least a head}, P(A) = ¾

For a population of size 30, using SRS, we select two individuals. There are 435 different choices. i.e. There are 435 outcomes in the sample space. Each one has probability 1/435 = 0.00229

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- How do I know there are 435 different choices?
- 435= (30x29)/2
- The first interview has 30 choices, the second has 29. (no repeats)
- But {John, Jane} is the same as {Jane, John}. This is the reason of dividing by 2

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counted as front pair] the probability is 9/1000. We write P(front pair) = 9/1000







Attendance Survey Question 10

- On a 4"x6" index card
 - Please write down your name and section number
 - Today's Question: Have You ever played

Pick 3 of Lotto Kentucky Powerball None of above

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