$\qquad$ Sec.: $\qquad$

Do not remove this answer page - you will turn in the entire exam. You have two hours to do this exam. No books or notes may be used. You may use an ACT-approved calculator during the exam, but NO calculator with a Computer Algebra System (CAS), networking, or camera is permitted. Absolutely no cell phone use during the exam is allowed.
The exam consists of multiple choice questions. Record your answers on this page. For each multiple choice question, you will need to fill in the circle corresponding to the correct answer. For example, if (a) is correct, you must write
(a) b c de

Do not circle answers on this page, but please circle the letter of each correct response in the body of the exam. It is your responsibility to make it CLEAR which response has been chosen. You will not get credit unless the correct answer has been marked on both this page and in the body of the exam.

## GOOD LUCK!

1. (a) b c d e
2. (a) b c d e
3. (a) b c d e
4. (a) b c d (e)
5. (a) b c d e
6. (a) b c d e
7. (a) b c d e
8. a b c d e
9. (a) b c d e
10. (a) b c d e
11. (a) b c d e
12. (a) b c d e
13. (a) b c d e
14. (a) b c d e
15. (a) b c d e
16. (a) b c d e
17. (a) b c d e
18. (a) b c d (e)
19. (a) b c d e
20. (a) b c d e

For grading use:

| Number <br> Correct |  |
| :---: | :---: |
|  | (out of 20 problems) |


$\qquad$

## Multiple Choice Questions

Show all your work on the page where the question appears. Clearly mark your answer both on the cover page on this exam and in the corresponding questions that follow.

1. The graph of two equations is shown below. Determine the number of solutions for the system of equations.

## Possibilities:

(a) 4
(b) 0
(c) 3
(d) 2
(e) 1

2. Use the substitution method to find all solutions of the system of equations.

$$
\begin{aligned}
& x+y^{2}=46 \\
& y-x=-4
\end{aligned}
$$

## Possibilities:

(a) $(x=10, y=6)$ only
(b) $(x=-3, y=-7)$ only
(c) $(x=-3, y=7)$ and $(x=11, y=-7)$
(d) $(x=-3, y=-7)$ and $(x=10, y=6)$
(e) No real solutions
3. Suppose you are solving the system of equations below using the substitution method. You solve for $y$ in the first equation and substitute it into the second equation. What equation must you solve then?

$$
\begin{aligned}
& 8 x^{7}+y=5 \\
& 4 x^{9}+3 y=6
\end{aligned}
$$

## Possibilities:

(a) $4\left(\sqrt[7]{5-8 x^{7}}\right)^{9}+3 y=6$
(b) $4 x^{9}+3(\sqrt[7]{5-y})=6$
(c) $4 x^{9}+3\left(5-8 x^{7}\right)=6$
(d) $4 x^{9}+3\left(\sqrt[7]{5-8 x^{7}}\right)=6$
(e) $4\left(5-8 x^{7}\right)^{9}+3 y=6$
4. Use the elimination method to solve the system. The multiple choice problem only asks you for $y$.

$$
\begin{aligned}
& 29 x+17 y=218 \\
& 29 x+16 y=212
\end{aligned}
$$

## Possibilities:

(a) Every solution has $y=\frac{6}{29}$
(b) Every solution has $y=6$
(c) Every solution has $y=4$
(d) Every solution has $y=-17$
(e) Every solution has $y=\frac{6}{17}$
5. Use substitution to solve the system.

$$
\begin{aligned}
& 5 x+3 y=13 \\
& 4 x+2 y=29
\end{aligned}
$$

## Possibilities:

(a) $x=-\frac{93}{2}, y=\frac{61}{2}$
(b) $x=152, y=110$
(c) $x=\frac{61}{2}, y=-\frac{93}{2}$
(d) $x=-\frac{1}{76}, y=-\frac{1}{55}$
(e) $x=\frac{13}{5}, y=\frac{29}{4}$
6. Use the elimination method to find all solutions of the system of equations.

$$
\left\{\begin{array}{l}
\frac{37}{x}+\frac{22}{y}=123 \\
\frac{17}{x}+\frac{11}{y}=58
\end{array}\right.
$$

## Possibilities:

(a) $(x=37, y=22),(x=-37, y=22),(x=17, y=11)$, and $(x=-17, y=-11)$
(b) $\left(x=\frac{3}{7}, y=\frac{3}{5}\right)$ only
(c) $(x=37, y=22)$ and $(x=17, y=11)$
(d) $(x=-37, y=22)$ and $(x=-17, y=11)$
(e) $\left(x=\frac{3}{7}, y=\frac{3}{5}\right)$ and $\left(x=-\frac{3}{7}, y=-\frac{3}{5}\right)$
7. Use algebraic, graphical, or numerical methods to find all real solutions of the equation, approximating when necessary to four decimal places.

$$
\frac{3 x}{x-20}=5
$$

## Possibilities:

(a) $x=50.0000$
(b) $x=50.1317$
(c) $x=50.2634$
(d) $x=50.3951$
(e) $x=50.5268$
8. Find an equation that helps solve for the worker's old salary, call it $x$, in the following problem: A worker gets a $5.35 \%$ pay raise and now makes $\$ 1350$ per month. What was the worker's old salary?

## Possibilities:

(a) $x=1350-5.35$
(b) $5.35 x=1350$
(c) $x=(5.35)(1350)$
(d) $0.0535 x=1350$
(e) $x+0.0535 x=1350$
9. You have already invested $\$ 700$ in a stock with an annual return of $10 \%$. How much of an additional $\$ 1,250$ should be invested at $20 \%$ and how much at $5 \%$ so that the total return on the entire $\$ 1,950$ is $15 \%$ ?

What equations should be solved if $x$ is the amount of money invested at $20 \%$ and $y$ is the amount of money invested at $5 \%$ ?

Possibilities:
(a) $\left\{\begin{array}{l}x=.20(1250) \\ y=.05(700)\end{array}\right\}$
(b) $\left\{\begin{array}{l}.05 x+.20 y=.10(1250) \\ .20 x+.05 y=.15(1950)\end{array}\right\}$
(c) $\left\{\begin{array}{rrr}x+y & = & 700 \\ .20 x+.05 y & = & .15(1950)\end{array}\right\}$
(d) $\left\{\begin{aligned} 700+x+y & =1950 \\ .10(700)+.20 x+.05 y & =.15(1950)\end{aligned}\right\}$
(e) $\left\{\begin{array}{rlr}.15+x+y & =1950 \\ 1250+.20 x+.05 y & = & .10(700)\end{array}\right\}$
10. A concrete walk of uniform width is to be built around a giant circular pool. The radius of the pool is 18 meters, and enough concrete is available to cover $64.09 \pi$ square meters (approximately). If all the concrete is to be used, how wide should the walk be (approximately)? Choose the closest answer.

## Possibilities:

(a) 46.1 meters wide
(b) 18 meters wide
(c) 9.99 meters wide
(d) 1.7 meters wide
(e) 3.56 meters wide
11. Find the equilibrium price. In the supply and demand equations, $p$ is price (in dollars) and $x$ is quantity (in thousands). Please round your answer to the nearest hundredth (the nearest cent).

$$
\begin{aligned}
\text { Supply: } & p=8 x-7 \\
\text { Demand: } & p=-4 x+9
\end{aligned}
$$

## Possibilities:

(a) $p=\$ 1.33$
(b) $p=\$ 3.66$
(c) $p=\$ 4$
(d) $p=\$ 6$
(e) $p=\$ 2$
12. A radiator contains 4 quarts of fluid, $25 \%$ of which is antifreeze. How much fluid should be drained and replaced with pure (100\%) antifreeze so that the new mixture is $65 \%$ antifreeze?

## Possibilities:

(a) 2.13 quarts drained and replaced
(b) 2.6 quarts drained and replaced
(c) 1 quarts drained and replaced
(d) 6.4 quarts drained and replaced
(e) 4 quarts drained and replaced
13. Solve the inequality. Answer in interval notation.
$6 x+18 \leq 5 x+20$
Possibilities:
(a) $[2, \infty)$
(b) $[3,4]$
(c) $(-\infty, 2]$
(d) $(-\infty, \infty)$
(e) $(-\infty, 6] \cup[18, \infty)$
14. A business executive is considering two options for leasing a car. The first option is $\$ 355$ per month, but the first month costs $\$ 90$ extra. The second option is $\$ 370$ per month with no extra cost for the first month. The business executive wants to know which option is cheapest based on how many months they plan on leasing the car. Which choice below most accurately describes the situation?

## Possibilities:

(a) The first option is cheaper if the lease is 14 months or shorter, the second option is cheaper if the lease is 16 months or longer, and the two options are the same price if the lease is exactly 15 months
(b) The first option is cheaper if the lease is 16 months or longer, the second option is cheaper if the lease is 14 months or shorter, and the two options are the same price if the lease is exactly 15 months
(c) Both options cost the same regardless of the length of the lease.
(d) The first option is cheaper if the lease is 7 months or longer, the second option is cheaper if the lease is 5 months or shorter, and the two options are the same price if the lease is exactly 6 months
(e) The first option is cheaper if the lease is 5 months or shorter, the second option is cheaper if the lease is 7 months or longer, and the two options are the same price if the lease is exactly 6 months
15. Solve the inequality. Express your answer in interval notation.

$$
\left|\frac{8}{9}+\frac{1}{9} x\right| \leq \frac{4}{9}
$$

## Possibilities:

(a) $[0,12]$
(b) $\left[\frac{4}{9}, \frac{8}{9}\right]$
(c) $[4,12]$
(d) $\left[0, \frac{4}{9}\right]$
(e) $[-12,-4]$
16. Solve the inequality. Answer by choosing the correct number line.

$$
0 \leq(x-8)(x-7)^{2}
$$

## Possibilities:

(a)

(b)

(c)

(d)

(e)

17. Solve the inequality. Answer by choosing the correct number line.
$0 \leq \frac{(x-8)(x-7)}{(x-4)(x-9)}$
Possibilities:
(a)

(b)

(c)

(d)

(e)

18. Find $f(-3)$ from the graph of $y=f(x)$.

## Possibilities:

(a) $f(-3)=-2$
(b) $f(-3)=0$
(c) $f(-3)=-4$
(d) $f(-3)=7$
(e) $f(-3)=-3$

19. Find the indicated value of the function when $x=\sqrt{3}+7$.

$$
f(x)=\sqrt{x+4}-x-9
$$

$f(\sqrt{3}+7)=$

## Possibilities:

(a) $\sqrt{\sqrt{3}+11}-\sqrt{3}-16$
(b) $\sqrt{11}-16$
(c) $\sqrt{\sqrt{3}+11}-\sqrt{3}-2$
(d) -5
(e) $\sqrt{14}-\sqrt{3}-16$
20. Let $f(x)=2 x^{2}+8$. Find $\frac{f(x+h)-f(x)}{h}$ if $h \neq 0$. Simplify your answer.

## Possibilities:

(a) $\frac{2 h^{2}+8}{h}$
(b) $4 x+2 h$
(c) 16
(d) $2 x+8 h$
(e) $\frac{h+16}{h}$

