## Circles, Arcs and Angles

MA 341 - Topics in Geometry Lecture 09

UK



## Star Trek Lemma

The measure of the inscribed angle is half of the angular measure of the arc it subtends.

There are several cases to the proof of the lemma. We will look only at the case where  $\angle BAC$  is an acute angle and the center, O, lies in the interior of the angle, as in our figure.

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## Inscribed Parallelograms A polygon is inscribed in a circle if all of its vertices lie on the circle and its interior is interior to the circle. Theorem: Opposite angles of an inscribed quadrilateral are supplementary.

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## Secants and Angles

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 Chords and Angles

 Theorem: The angle between two chords is equal to half the sum of the two subtended arcs.

  $\angle AXB = \frac{1}{2}(\widehat{AB} + \widehat{CD})$  

 A 

 O 

 X 

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 X 

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