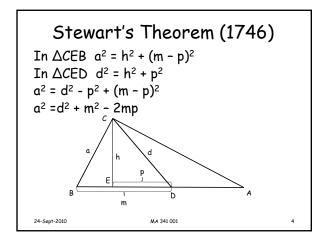
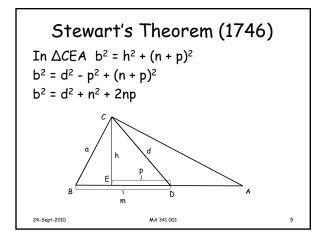


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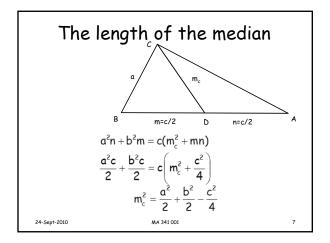
Stewart's Theorem (1746)

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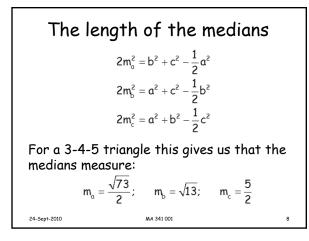
6

 $a^{2}n = d^{2}n + m^{2}n - 2mnp$ $b^{2}m = d^{2}m + n^{2}m + 2mnp$ $a^{2}n + b^{2}m = d^{2}n + m^{2}n + d^{2}m + n^{2}m$ $= d^{2}(n + m) + mn(m + n)$ $a^{2}n + b^{2}m = c(d^{2} + mn)$

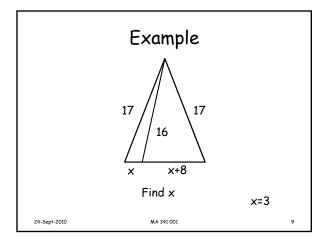
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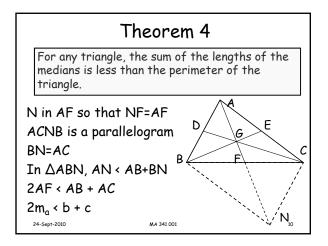




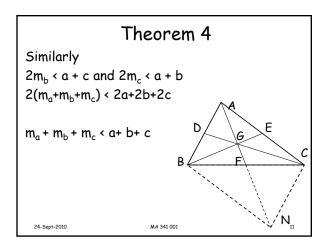




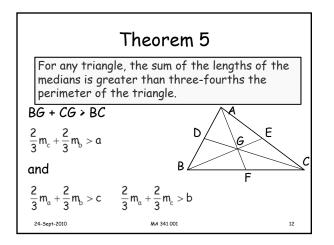




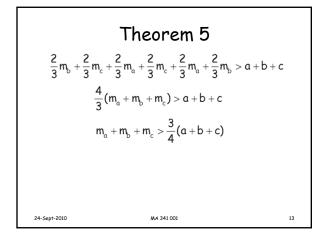




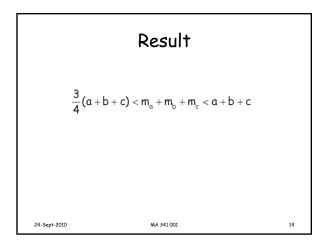


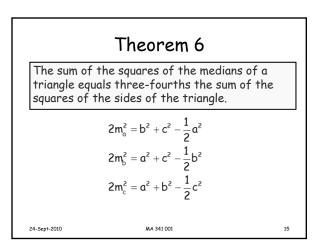




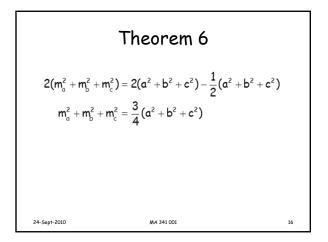




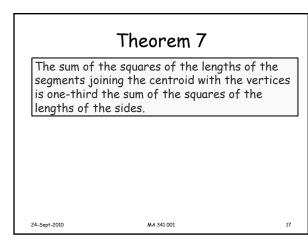


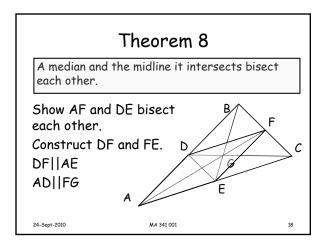




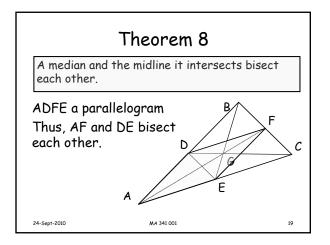




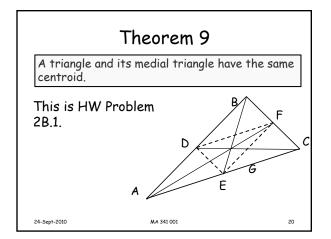




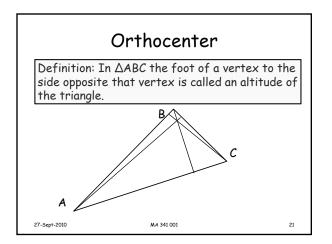




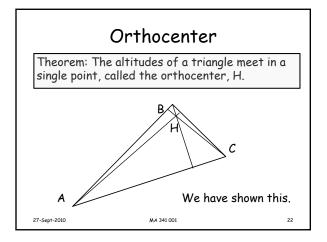




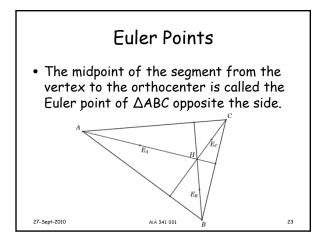




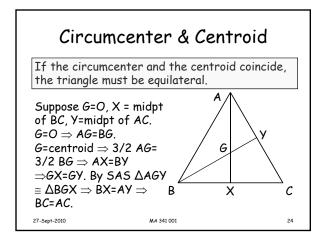




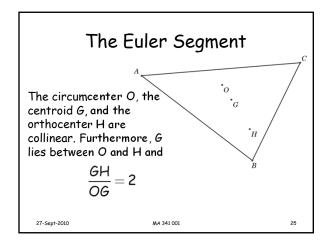




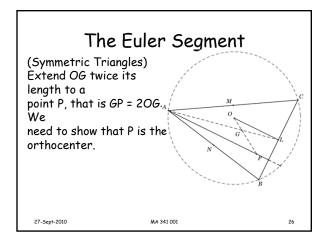


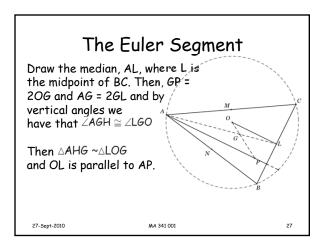














The Euler Segment

Since OL is perpendicular to BC, so it AP, making P lie on the altitude from A.

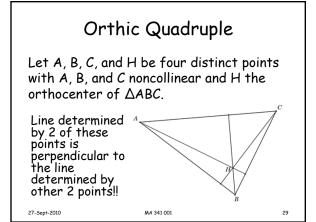
Repeating this for each of the other vertices gives us our result. By construction GP = 20G.

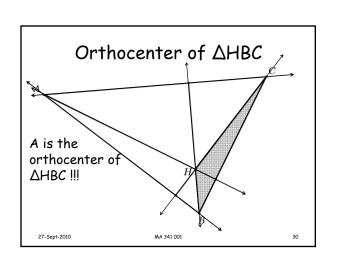
This line segment is called the $\underline{\mbox{Euler Segment}}$ of the triangle.

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Orthic Quadruple

- H is the orthocenter of ΔABC
- A is the orthocenter of ΔHBC
- B is the orthocenter of ΔHAC
- C is the orthocenter of ΔHAB

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{A, B, C, H} is called Orthic Quadruple

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Orthic Quadruple Given three points {A, B, C} there is always a fourth point, H, making an orthic quadruple UNLESS 1. A, B, C collinear 2. A, B, C form a right triangle

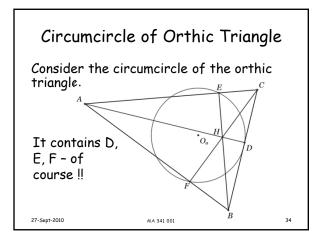
Orthic Triangle

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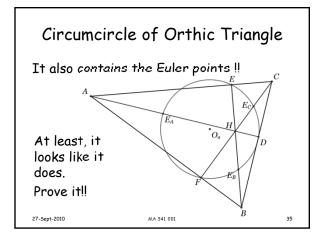
Let A, B, C form a triangle and let D, E, F denote the intersections of the altitudes from A, B, and C with the lines \overrightarrow{BC} , \overrightarrow{AC} , and \overrightarrow{AB} respectively. The triangle DEF is called the orthic triangle.

Theorem: The orthic triangles of each of the four triangles determined by an orthic guadruple are all the same.

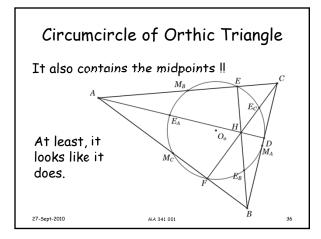
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Nine Point Circle Theorem

Theorem: For any triangle the following nine points all lie on the same circle: the three feet of the altitudes, the three Euler points, and the three midpoints of the sides. Furthermore, the line segments joining an Euler point to the midpoint of the opposite side is a diameter of this circle.

Sometimes called Feuerbach's Circle.

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