Name: Answer Rey Section:003

MA 201-003: Exam III

Please read the following carefully.

- There are 10 questions on this exam and there are 10 points possible for each question. The exam is worth 100 points total.
- You may not use a calculator.
- For any question which asks you to explain something you must write in complete English sentences. You can lose points for incomplete or incomprehensible explanations.
- For any computation problem you must show all work. You will lose points if it is not made clear how you arrive at an answer.
- Follow all instructions carefully. If a problem says to use a particular method, you must use that method. No points can be awarded if you fail to use the specified method.
- Relax and don't spend too much time on any one problem! Good luck.

Question	Possible	Earned
1	10	
2	10	
3	10	
4	10	
5	10	
6	10	
7	10	
8	10	
9	10	
10	10	
Total:	100	

1. §3.1

(a) Write 2,572 in expanded notation. (2 pts)

2x1,000 + 5x100 + 7x10+ ax1

(b) What is 134 in heiroglyphics. (2 pts)

9000 1111

(c) What number is CMLXIII? (2pt)

900 | 50 | 10 | 3

(d) Fill in the box with <,=,>: (Show your work by first converting each to our number system.) (4 pts)

2000 10 50 9 2000 900 50 9

2016 12 1959

TABLE 3.1 Egyptian Symbols for Powers of 10

Power of 10 $10^0 = 1$ $10^1 = 10$ $10^2 = 100$ $10^3 = 1000$ $10^4 = 10,000$ $10^5 = 100,000$ $10^6 = 1,000,000$

Egyptian Symbol Description

a staff a yoke a scroll a lotus a pointing a fish an amazed person

TABLE 3.2 Roman Numerals and Their Modern Equivalents

 Roman Symbol
 1
 V
 X
 L
 C
 D
 M

 Modern Equivalent
 1
 5
 10
 50
 100
 500
 1000

2. §5.1

For the following questions let • represent a positive integer, and o represent a negative integer, as in colored counters.

(a) Write down the set of all integers in list notation. (2 pts)

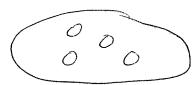
$$\{1, -2, -1, 0, 1, 2, ...\}$$

(b) What property is shown here: 7 + (-7) = 0 (1 pt)

(c) Demonstrate the number 3 in two different ways using colored counters. (2 pts)



(d) Represent the number -4 using colored counters. (1 pt)

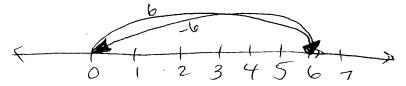


(e) If you receive a bill for \$30 and a check for \$50, did your net worth increase or decrease? By how much? (Be sure to write the correct equation before you solve.) (2 pts)

$$30+(-50)=-20$$

\$20 decrease

(f) Demonstrate 6 + (-6) using a numberline. (1 pt)

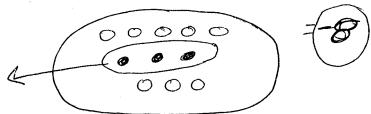


head to

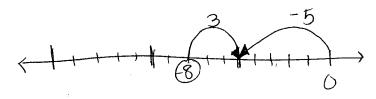
- (g) Fill in the box with <, =, >. (1 pt)
 - (a) $|7| \square |-3|$



- 3. §5.2 For the following questions let represent a positive integer, and o represent a negative integer, as in colored counters.
 - (a) Draw a diagram using colored counters for -5 (3) and solve. (2pts)



(b) Solve -5 - (3) using a number line. (2pts)



- heads together
- (c) The mailman brings a check for \$11, a bill for \$3 and another bill for \$4. Are you richer or poorer? By how much? (Be sure to write the correct equation before you solve.) (2pts)

$$11+(-3)+(-4)=11-7=4$$
(\$4 richer

(d) The mailman brings you a check for \$11 and takes away a bill for \$6. Are you richer or poorer? By how much? (Be sure to write the correct equation before you solve.) (2pts) (2pts)

$$11-(-6)=17$$
(\$17 richer)

(e) Write the mail-time story for the following subtraction and solve it. (2 pts)

$$(-5) - 4$$

The mailman brings a bill for \$5 and takes a cheek



4. §5.3

(a) Fill in the boxes with either a + or a - sign. (We are assuming that m, n are both positive integers. When you see -m, that will represent a negative integer, and +m represents a positive integer, for example.) (2pts)

(a)
$$(+m) \cdot (+n) = \Box mn$$

(b)
$$(-m) \cdot (+n) = \square mn$$

(c)
$$(+m) \cdot (-n) = \square mn$$

(d)
$$(-m) \cdot (-n) = \Box mn$$

(e) The letter carrier takes away 4 bills for \$16 each. Are you richer or poorer? By how much? (Be sure to write the correct equation before you solve.) (2pts)

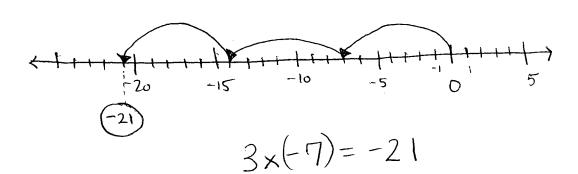
(f) Complete the following divisions: (3pts)

(a)
$$12 \div (-4) = -3$$

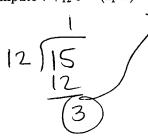
(b)
$$-51 \div (-17) = 3$$

(c)
$$-8 \div (2) = -4$$

(d) What product does this diagram illustrate? (3pts)



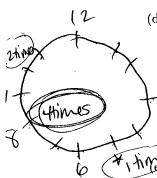
(a) Compute $7 +_{12} 8 = (2pts)$



(b) Compute 5 - 12 7 = (2pts)

- (c) Lacey went out to go shopping on Black Friday. She got home at 6. 00pm. She left to go shopping 11 hours ago. What time did Lacey leave to go shopping this morning? (2pts)

$$6-_{12}11 = 6+1 = 7.00AM$$



(d) Compute $8 \div_{12} 5 = (2pts)$

8x25=40)=14

(4) or go around the Bap clock \$5pots 4 times to

$$8 \times 4 = 32$$
 10132
 30
 (2)



6. §6.1 Modeling Fractions/Equivalent Fractions

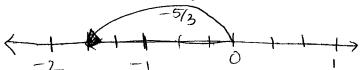
Be sure to identify your units on the following problems.

(a) How many different representations are there for the fraction $\frac{1}{2}$? (1pt)

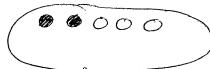
(b) Represent the fraction $\frac{1}{6}$ using the colored region model. (1pt)



(c) Represent the fraction $\frac{-5}{3}$ using the number line model. (1pt)



(d) Represent the fraction $\frac{2}{5}$ using the set model. (1pt)



2 out of 5 circles are Shaded. My unit is 5 circles.

(e) Represent the fraction $1\frac{3}{5}$ using fraction strips. (2pts)



(f) State the Cross-Product Property of Equivalent Fractions given that $\frac{a}{h}$ and $\frac{c}{d}$ are fractions. (In other words, how do we know when $\frac{a}{b} = \frac{c}{d}$?) (2pts)

$$\frac{\alpha}{b} = \frac{c}{d} \iff ad = bc$$
.

(g) Is $\frac{14}{6} = \frac{17}{8}$? Explain. (2pts)

Can see that 14x8 \$ 6x17 because

112 7 102 OR:

Common denom:

$$\frac{14}{6} = \frac{14}{6} \times \frac{4}{4} = \frac{56}{24}$$

$$\frac{17}{8} = \frac{17}{8} \times \frac{3}{3} = \frac{51}{24}$$

and 56 \$ 51.

7. §6.1 Simplifying fractions/Common Denominators/Ordering

(a) Write $\frac{24}{72}$ in simplest terms. Explain how you know it is in simplest terms. (2 pts)

$$\frac{24}{-72} = \frac{12}{-36} = \frac{6}{-18} = \frac{3}{-9} = \frac{1}{-3} = \left(-\frac{1}{3}\right)$$

This is in simplest terms because the denominator is positive and gcd(-1,3)=1.

$$\frac{294}{84} = \frac{\cancel{3} \cdot \cancel{3} \cdot \cancel{7}}{\cancel{2}^{\cancel{2}} \cdot \cancel{3} \cdot \cancel{7}} = \frac{\cancel{7}}{\cancel{2}^{\cancel{2}} \cdot \cancel{3} \cdot \cancel{7}} = \frac{\cancel{7}}{\cancel{2}}$$

(c) Explain in 2-3 sentences how to get two equivalent fractions but with a common denominator for the fractions $\frac{2}{7}$ and $\frac{5}{21}$. (3pts)

Since 21 is a multiple of 7, we can leave $\frac{5}{21}$ as it is. Then, ask ourselves "what should we multiply 7 by to get 21?". Since we must multiply by a form of 1 we multiply by $\frac{3}{3}$. $\frac{2}{7} \times \frac{3}{3} = \frac{6}{21}$.

(d) Show that $\frac{a}{b} < \frac{c}{d}$ when ad < bc. (3pts)

Get a common denominator

$$\frac{a}{b} \times \frac{d}{d} = \frac{ad}{bd}$$

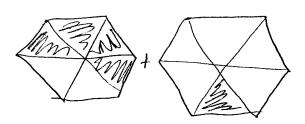
$$\frac{C}{d} \times \frac{b}{b} = \frac{bc}{bd}$$
.

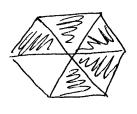
So, our two fractions are $\frac{5}{21}$ and $\frac{6}{21}$.

and because ad < bc we put < everywhere. So that 9/b/c/d.

8. §6.2 Adding and Subtracting Fractions/Mixed Numbers vs. Proper Fractions

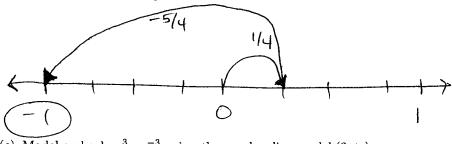
(a) Model and solve $\frac{4}{6} + \frac{1}{6}$ using the shaded region model. (1pt)



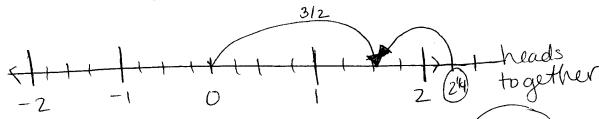




(b) Model and solve $\frac{1}{4} + \frac{-5}{4}$ using the number-line model. (2pts)



(c) Model and solve $\frac{3}{2} - \frac{-3}{4}$ using the number-line model. (3pts)



(d) Give an improper fraction for $3\frac{8}{9}$. (Show your work.) (2pts)

$$38/9 = \frac{(3 \times 9) + 8}{9} = \frac{27 + 8}{9} = \frac{35}{9}$$

(e) Compute
$$2\frac{1}{4} + 5\frac{2}{5}$$
. (Show your work.) $(2pts) = 2+5+\frac{1}{4}+\frac{2}{5} = 7+\frac{5}{20}+\frac{8}{20}=\frac{213}{27}$

$$(2\times4)+1+(5\times5)+2=9+27$$

$$(2\times4)+1+(5\times5)+2=9+27$$

$$(2\times4)+1+(5\times5)+2=9+27$$

$$(3\times5)+2\times5$$

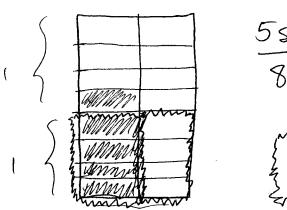
$$\frac{9x5}{4x5} = \frac{45}{20}$$

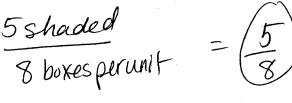
$$\frac{27}{5} \times \frac{4}{4} = \frac{108}{20}$$

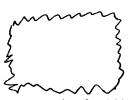
$$\frac{45}{20} + \frac{108}{20} = \frac{153}{20} = \frac{7}{20}$$

9. §6.3 Multiplying Fractions

(a) Using the rectangular area model, compute $\frac{5}{4} \times \frac{1}{2}$. (4 pts)







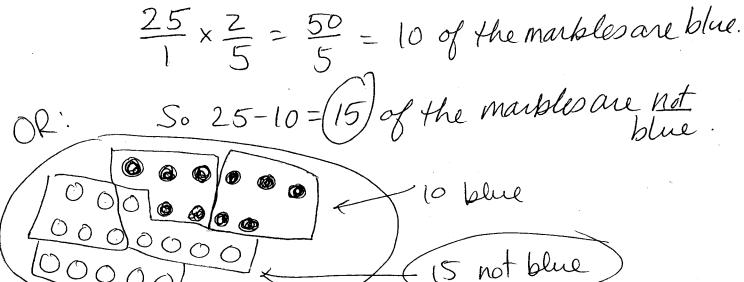
indicates the unit.

(b) You need to carpet a room that is 100 inches by 144 inches. The carpet store sells their carpet in square feet. The carpet is \$8 per square foot. How much money do you have to spend on carpet, assuming you buy exactly enough? (There are 12 inches in a foot.) (3pts)

100 x 144 = 100x1 = 100 square feet needed.

\$8 x 100 = \$800 per sign for carpet

(c) A bag contains 25 marbles. If $\frac{2}{5}$ of the marbles are blue, how many marbles are not blue? (3pts)



10. §6.3 Dividing Fractions

(a) The following is a proof that $\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{c}{d}$. Beside each step, justify why each step is valid. (The first line has been done for you.) We start by knowing that $f(\frac{a}{b} \div \frac{c}{d} = \frac{e}{f})$ then we also have $\frac{a}{b} = \frac{e}{f} \times \frac{c}{d}$. (4pts)

Diven above $\frac{a}{b} = \frac{e}{f} \times \frac{c}{d}$

$$\frac{a}{b} = \frac{e}{f} \times \frac{c}{d}$$

$$h \text{ Sides by } \frac{d}{c} \Rightarrow \frac{a}{b} \times \frac{d}{c} = \left(\frac{e}{f}\frac{c}{d}\right)\frac{d}{c}$$

$$\frac{c}{d} \times \frac{d}{c} = 1$$

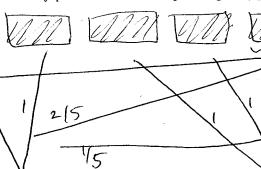
$$\Rightarrow \frac{a}{b} \times \frac{d}{c} = \frac{e}{f}$$

$$\frac{e}{f} = \frac{a}{b} \div \frac{c}{d}$$
 by

by
$$\Rightarrow \frac{a}{b} \times \frac{d}{c} = \frac{a}{b} \div \frac{c}{d}$$

Therefore
$$\frac{a}{b} \times \frac{d}{c} = \frac{a}{b} \div \frac{c}{d}$$
.

(b) Draw a diagram to represent and solve the problem: Suzy, Tiffany, and Rachel want to share $7\frac{4}{5}$ pounds of apples. If they decide to distribute the apples evenly, how many pounds should each person get? (4pts)



215

45

each gets

(c) Compute the following and leave your answer in simplest form: (2pts)

(a)
$$\frac{3}{5} \div \frac{6}{11}$$

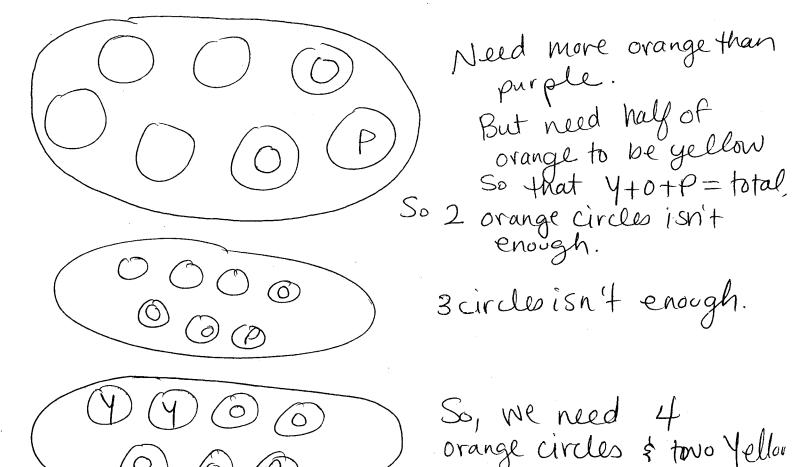
$$\frac{3}{5} \times \frac{11}{62} = \frac{11}{10}$$

(b) $\frac{-4}{5} \div \frac{8}{9}$

$$\frac{-4}{5} \times \frac{9}{8} = \left(\frac{-9}{10}\right)$$

EXTRA CREDIT

(a) A bag contains yellow, orange and purple marbles. One-seventh of the marbles are purple. There are fifteen more orange marbles than purple marbles. There are half as many yellow marbles as orange marbles. How many marbles are there of each color? (You may use any method you'd like to answer this problem.) (5pts)



But how many in each?

We know that Orange marbles are 15 more than purple. So, because there are 3 extra orange circles, 3 orange circles makes up 15 marbles. This means there are 5 marbles per circle. So P=5 0=20 Y=10.