

Def: constants - describe static situations in which change is not under consideration. (eg. 12 in a dozen,  $2 + 5 = 7$ )

Def: variables - changeable quantities

Ways variables are used:

- to describe generalized properties:  $a + (b + c) = (a + b) + c$  for all real  $a, b, c$ .  
(Here  $a, b, c$  are generalized variables - they represent an arbitrary member of a set)
- to express relationships: Jolie was born on her 3-year old sister Kendra's birthday. How are their ages related? ( $J = K - 3, K = J + 3, K - J = 3$ )
- to serve as unknowns in equations:  $\square + 5 = 9, (2x - 6)(x - 1) = 0$
- to express formulas:  $d = rt, A = lw, P = 2l + 2w$

p. 496 #2: In each situation below, classify the role of the variables as one of the following types: generalized; expressing a relationship; expressing a formula; an unknown.

- (a) For all real numbers  $x, y, z$ :  $x(y + z) = xy + xz$      ◆ Generalized variables
- (b) Elena is 4 inches shorter than her husband, Joe, so  $E = J - 4$ .     ◆ Expressing a relationship
- (c) To construct a circular flower bed covering 400 square feet of ground, the radius  $r$  of the bed must satisfy  $\pi r^2 = 400$ .     ◆ Unknown
- (d) Tickets to the play are \$5 for adults and \$3 for children. If  $A$  adults and  $C$  children attend the play, the total proceeds are  $5A + 3C$ .     ◆ Expressing a formula

Def: numerical expression - any representation of a number that involves numbers and operation symbols. ( $3 + 8$ )

Def: algebraic expression - an expression involving variables, numbers and operation symbols. ( $4x + 8y$ )

p. 496 #4: Penny is  $p$  years old. Form algebraic expressions with the variable  $p$  that represent the ages requested.

- (a) Penny's age in 5 years ( $p + 5$ )
- (b) Penny's age 8 years ago ( $p - 8$ )
- (c) The *current* age of Penny's little brother, who in two more years will be half of Penny's age. ( $\frac{1}{2}(p+2) - 2$ )
- (d) The *current* age of Penny's mother, who, three years ago was 4 times Penny's age. ( $4(p - 3) + 3$ )

Def: domain of a variable - the set of all values for which the expression is meaningful.

Def: to evaluate an expression - to replace all the variables with particular values.

Def: equation - two algebraic expressions with the same value

There are two types of equations:

Def: identity equation - an equation that is true for all evaluations of the variables. ( $(x + y)^2 = (x^2 + 2xy + y^2)$ )

Def: conditional equation - an equation that is true only for specific evaluations of the variables. ( $a^2 + b^2 = c^2$ )

Def: solution set - the set of all values in the domain of the variables that satisfy the given equation.

Def: equivalent equations - two equations that have the same solution set.

We use equivalent equations to simplify equations. You must be careful though, as some operations are not completely equivalent.

Def: function on a set  $D$ - a rule that associates each element  $x \in D$  precisely one value  $y$ .

Def: domain of a function - the set on which the function is defined ( $D$  in the above definition).

We typically use letters or words to name the function.  $f(x)$ ,  $\text{sqrt}(z)$ , etc.

Functions can also be thought of as a set of ordered pairs  $\{(x,y)|x \in D \text{ and } y = f(x)\}$ . We can then use the Vertical Line Test to check if it is a function.

Def: image or value of  $f$  at  $x$ - what comes out of the function when you plug  $x$  in.

Def: range of a function - the set of all images of  $f$  on  $D$ . (range  $f = \{y|y = f(x) \text{ for some } x \in D\}$ )

Example 8.3: Let  $f$  be the function defined by the formula  $f(x) = x(10 - x)$  on the domain  $D = \{1, 3, 5, 7, 9\}$ .

|        |   |    |    |    |   |
|--------|---|----|----|----|---|
| $x$    | 1 | 3  | 5  | 7  | 9 |
| $f(x)$ | 9 | 21 | 25 | 21 | 9 |

The range of  $f$  is  $\{9, 21, 25\}$ .

Example 8.4: Guess the rule

|        |    |   |    |    |    |
|--------|----|---|----|----|----|
| $x$    | 2  | 5 | 6  | 0  | 1  |
| $f(x)$ | -1 | 8 | 11 | -7 | -4 |

$f(x) = 3x - 7$

|        |    |   |    |    |    |    |
|--------|----|---|----|----|----|----|
| $x$    | 5  | 2 | 4  | 0  | -2 | -5 |
| $f(x)$ | 24 | 3 | 15 | -1 | 3  | 24 |

$f(x) = x^2 - 1$

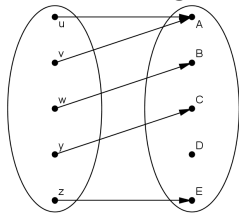
Ways to describe or visualize functions:

- as formulas:  $A(r) = \pi r^2$ ,  $f(n) = f_n = \frac{n(n+1)}{2}$   
(Functions defined on  $\mathbb{N}$  are called sequences)

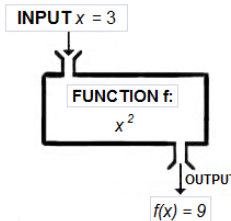
- as tables:

|         |   |   |    |
|---------|---|---|----|
| Student | A | B | C  |
| Grade   | 8 | 7 | 10 |

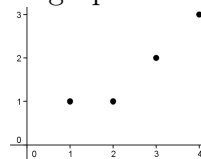
- as arrow diagrams



- as machines



- as graphs



Note: Functions of the form  $f(x) = mx + b$  are called linear functions.

Section 8.1 HW: #3, 10, 13, 17, 20, 21, 24, 29, 32, 45 (part of HW1)