## MA 114 Worksheet #01: Substitution Review

1. Evaluate the following indefinite integrals and indicate the substitutions that you use.

(a) 
$$\int \frac{4}{(1+2x)^3} dx$$
  
(b) 
$$\int x^2 \sqrt{x^3+1}$$
  
(c) 
$$\int \cos^4 x \sin x \, dx$$
  
(d) 
$$\int \sec^3 x \tan x \, dx$$
  
(e) 
$$e^x \sin(e^x)$$
  
(f) 
$$\frac{2x+3}{x^2+3x}$$

2. Evaluate the following definite integrals and indicate the substitutions that you use.

(a) 
$$\int_{0}^{7} \sqrt{4+3x} \, dx$$
  
(b)  $\int_{0}^{\frac{\pi}{2}} \cos(x) \cos(\sin(x)) \, dx$   
(c)  $\int_{0}^{3} \frac{dx}{6x+1}$   
(d)  $\int_{-\pi/3}^{\pi/3} x^{4} \sin x \, dx$   
(e)  $\int_{0}^{1} \frac{e^{z}+1}{e^{z}+z} \, dz$   
(f)  $\int_{0}^{4} \frac{x}{\sqrt{1+2x}} \, dx$ 

- 3. If f is continuous and  $\int_0^6 f(x) = 8$ , find  $\int_0^2 f(3x)$ .
- 4. If f is continuous and  $\int_0^{25} f(x) dx = 16$ , find  $\int_0^5 x f(x^2) dx$ .
- 5. Find the area of the region between the graphs of  $y = x^2$  and  $y = x^4$ .
- 6. Find the area of the regions enclosed by the graphs of  $y = \sqrt{x}$  and  $y = \frac{1}{4}x + \frac{3}{4}$  in two ways.
  - (a) Write this as an integral in x.
  - (b) Solve each equation to express x in terms of y and write an integral with respect to y.
- 7. Find the area of the region enclosed by the graphs of y = x + 1 and  $y = x^3 + x^2 x + 1$ .
- 8. What is the area of the region bounded by  $f(x) = \frac{1}{x}$ ,  $x = e^2$ ,  $x = e^8$  and x-axis? Sketching the region might be helpful.
- 9. If f is continuous on [0, 1], show that

$$\int_0^1 f(x)dx = \int_0^1 f(1-x)dx.$$

10. Find the area of the region bounded by the parabola  $y = x^2$ , the tangent line to the parabola at (1, 1) and the x-axis.