

## MA 114 Worksheet #11: Comparison & Limit Comparison Tests

1. (a) Explain the test for divergence. Why should you never use this test to prove that a series converges?
 

(b) State the comparison test for series. Explain the idea behind this test.

(c) Suppose that the sequences  $\{x_n\}$  and  $\{y_n\}$  satisfy  $0 \leq x_n \leq y_n$  for all  $n$  and that  $\sum_{n=1}^{\infty} y_n$  is convergent. What can you conclude? What can you conclude if instead  $\sum_{n=1}^{\infty} y_n$  diverges?

(d) State the limit comparison test. Explain how you apply this test.
2. Use the appropriate test — Divergence Test, Comparison Test or Limit Comparison Test — to determine whether the infinite series is convergent or divergent.

(a)  $\sum_{n=1}^{\infty} \frac{1}{n^{3/2} + 1}$

(h)  $\sum_{n=0}^{\infty} \frac{n+1}{n^2 \sqrt{n}}$

(b)  $\sum_{n=1}^{\infty} \frac{2}{\sqrt{n^2 + 2}}$

(i)  $\sum_{n=0}^{\infty} \frac{2}{\sqrt{n^2 + 2}}$

(c)  $\sum_{n=1}^{\infty} \frac{2^n}{2 + 5^n}$

(j)  $\sum_{n=0}^{\infty} \frac{n^2 + n + 1}{3n^2 + 14n + 7}$

(d)  $\sum_{n=0}^{\infty} \frac{4^n + 2}{3^n + 1}$

(k)  $\sum_{n=0}^{\infty} \frac{1 + 2^n}{2 + 5^n}$

(e)  $\sum_{n=0}^{\infty} \frac{n!}{n^4}$

(l)  $\sum_{n=0}^{\infty} \frac{2}{n^2 + 5n + 2}$

(f)  $\sum_{n=0}^{\infty} \frac{n^2}{(n+1)!}$

(m)  $\sum_{n=0}^{\infty} \frac{e^{1/n}}{n}$

(g)  $\sum_{n=0}^{\infty} \left(\frac{10}{n}\right)^{10}$

(n)  $\sum_{n=0}^{\infty} \frac{n}{n^2 - \cos^2 n}$