## Names:

I. Bert, Ernie and Grover have won a ride in a rocket, but only one of them will get to ride. They decide to give the ride to the highest bidder, and that whoever takes the ride should compensate the others equitably. Bert thinks the ride is worth \$900; Ernie bids \$630, and Grover (who is a little bit afraid of heights) bids $\$ 270$.

1. Find the fair shares for each person.
2. Who could possibly get the ride if we require a fair settlement? Explain briefly. (Hint: begin by computing the average of the bids.)
3. Give any example of an envy-free settlement. (Hint: find the range of possible payments, and then pick one.)
II. Kermit and Miss Piggy are getting a divorce! They have several assets to divide which they can't agree on, and decide to use the Adjusted Winner method to divide them fairly. Show the steps and give the final settlement.

|  |  | Kermit | Piggy |
| :---: | :--- | :---: | :---: |
| A. | framed artwork | 15 | 20 |
| B. | Rolls Royce | 30 | 10 |
| C. | NY apartment | 45 | 30 |
| D. | Paris apartment | 10 | 40 |

III. James Bond, Moneypenny, M, and Q have to divide a collection including a poisoned pen, a magnetic-resistant watch, and an underwater jet-pack. They each value the items as shown.
Here is the settlement they come

|  | Bond | Moneypenney | M | Q |
| :--- | ---: | ---: | ---: | ---: |
| pen | 100 | 300 | 400 | 500 |
| watch | 500 | 500 | 400 | 600 |
| jet-pack | 900 | 100 | 200 | 800 |

Total
Fair share up with:

Suppose that Bond takes the jet-pack and pays $\$ 500, M$ takes the pen and receives $\$ 100, Q$ takes the watch and pays $\$ 200$, and Moneypenney receives $\$ 600$.

1. Find $x_{\text {Bond }}, x_{\text {Moneypenney }}, x_{\mathrm{M}}$ and $x_{\mathrm{Q}}$.
2. Is this settlement fair? Explain.
3. How much is Bond's settlement worth to Q ? Does Q envy Bond?
4. Compute the XB ratios for Bond and for M.
IV. More practice
a. For problem I (Bert, Ernie and Grover), find a settlement that is equitable. (Hint: use the equitability method). Show steps clearly.
b. For problem I part 3 (your envy-free settlement), how would you justify that your settlement is envy-free? (Explain the process.)
c. For problem I part 3, is your envy-free settlement also equitable? Explain why or why not. Include calculations.
d. For problem III (James Bond, Moneypenny, M, and Q), find a settlement using Knaster's method. Use your own paper to work out the calculations; give just the final settlement here:
