

SOLUTIONS

Now suppose we have an election between Arya (A), Bran (B), and Jon (J).

	6	5	3	7
1 <sup>st</sup>	A	B	B	J
2 <sup>nd</sup>	J	A	J	B
3 <sup>rd</sup>	B	J	A	A

1. Find the winner using Plurality with Elimination.

21 voters, need 11 for majority.  
No maj. candidate, so eliminate A:

6	5	3	7
J	B	B	J
B	J	J	B

winner is Jon with 13

Now suppose the three voters in the third column change their votes: they pick 1<sup>st</sup> Jon, 2<sup>nd</sup> Bran, and 3<sup>rd</sup> Arya.

2. Draw the new preference schedule which reflects this change. Is this change an appropriate way to test monotonicity? Explain.

6	5	③	7
A	B	J	J
J	A	B	B
B	J	A	A

The winner was Jon.  
The new ballot moves Jon up, and keeps B and A in the same order as before.

This is an appropriate test.  
(regardless of whether winner changes.)

3. Find the winner using plurality with elimination.

No maj. cand; fewest 1<sup>st</sup> place votes is B with 5:

Elim B:

6	5	3	7
A	A	J	J
J	J	A	A

Now A Wins with 11 votes.

(This example shows that plur. w/elim) can fail the monotonicity criteria.)

4. Suppose instead, from the original election, that the six voters in the first column changed their votes to pick 1<sup>st</sup> Bran, 2<sup>nd</sup> Jon, and 3<sup>rd</sup> Arya. Is this change an appropriate way to test monotonicity? Explain.

old votes	new votes
<u>6</u>	<u>6</u>
A	B
J	J
B	A

No: The change does NOT move the winner (J) up. Also, it scrambles A and B (non winners). Either of these are reasons it would not work.