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1. Suppose we have a linear transformation $T: \mathbb{R}^{2} \rightarrow \mathbb{R}^{5} . T$ sends $\mathbf{e}_{1}$ to the vector $(1,2,3,4,5)$ and $\mathbf{e}_{2}$ to the vector $(1,-1,1,-1,1)$. Write the standard matrix $A$ for $T$. Then find $T\left(\left[\begin{array}{l}2 \\ 3\end{array}\right]\right)$.
2. Suppose a transformation $T: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$ reflects vectors about the vertical $y$ (or $x_{2}$ ) axis. Find the associated matrix $A$. Show work (by using graphs showing what $T$ does to $\mathbf{e}_{1}$ and $\mathbf{e}_{2}$ ).
3. Let $A=\left[\begin{array}{lll}1 & 2 & 3 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \\ 0 & 0 & 0\end{array}\right]$ and let $T(\mathbf{x})=A \mathbf{x}$.
a. If $T: \mathbb{R}^{a} \rightarrow \mathbb{R}^{b}$, find $a$ and $b$.
b. Is this transformation one-to-one? Justify briefly.
c. Is this transformation onto? Justify briefly.
