

1. Find the \mathcal{B} -coordinate vector of $\mathbf{x}_1 = \begin{bmatrix} 5 \\ 4 \end{bmatrix}$ relative to the basis $\mathcal{B} = \left\{ \begin{bmatrix} -3 \\ 4 \end{bmatrix}, \begin{bmatrix} -5 \\ 6 \end{bmatrix} \right\}$.

2. Let $T: \mathbb{R}^3 \rightarrow \mathbb{R}^3$ be the linear transformation represented by $T(x_1, x_2, x_3) = (2x_3, x_2, 0)$.

a. Find the standard matrix A which is associated to T .

b. Is A diagonalizable? If so, find P and D so that $A = PDP^{-1}$:

i. Find the eigenvalues associated to A .

ii. Find the associated eigenvectors for those eigenvalues.

iii. Find P and D (or explain why it is not possible).