We introduce the basic functions that we will consider throughout

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 polynomial functions $f(x) = a_0 + a_1x + a_2x^2 + \cdots + a_nx^n$

the remainder of the semester

Basic Functions

A polynomial function is a function of the form where n is a nonnegative integer and a_0, a_1, \ldots, a_n are (real) constants with $a_n \neq 0$. The coefficient a_n is called the leading coefficient, and n is called the degree of the polynomial

function. The largest possible domain of f is \mathbb{R} . Examples Suppose a, b, c, and m are constants.

- Constant functions: f(x)=c (graph is a horizontal line):
- Linear functions: f(x) = mx + b (graph is a straight line): • Quadratic functions: $f(x) = ax^2 + bx + c$ (graph is a parabola).

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Basic Functions

rational functions

A rational function is the quotient of two polynomial functions p(x) and q(x): $f(x) = \frac{p(x)}{q(x)}$ for $q(x) \neq 0$.

Example The Monod growth function is frequently used to describe

the per capita growth rate of organisms when the rate depends on the concentration of some nutrient and becomes saturated for large enough nutrient concentrations.

by N, then the per capita growth rate r(N)is given by $r(N) = \frac{aN}{k+N}, \quad N \ge 0$ where a and k are positive constants.

a/2

power functions

A power function is of the form $f(x) = x^r$ where r is a real number.

Example Power functions are frequently found in "scaling relations" between biological variables (e.g., organ sizes). Finding such relationships is the objective of allometry. For example, in a

study of 45 species of unicellular algae, a relationship between cell volume and cell biomass was sought. It was found [see, Niklas (1994)] that cell biomass ∝ (cell volume)0.794

Most scaling relations are to be interpreted in a statistical sense; they are obtained by fitting a curve to data points. The data points are typically scattered about the fitted curve

 exponential and logarithmic functions trigonometric functions

given by the scaling relation.

Lecture 2

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If we denote the concentration of the nutrient