MA 213 — Calculus III Fall 2017 Exam 2 October 18, 2017

## Exam Scores

Do not write in the table below

Section:		

Name: \_\_\_\_\_

Last 4 digits of student ID #: \_\_\_\_\_

- No books or notes may be used.
- Turn off all your electronic devices and do not wear ear-plugs during the exam.
- You may use a calculator, but not one which has symbolic manipulation capabilities or a QWERTY keyboard.
- Additional blank sheets for scratch work are available upon request.
- All questions are free response questions. Show all your work on the page of the problem. Clearly indicate your answer and the reasoning used to arrive at that answer. Unsupported answers may not receive credit.

Question	Score	Total
1		8
2		9
3		8
4		8
5		9
6		9
7		9
8		9
9		10
10		10
11		11
Total		100

**1.** (8 points) Use polar coordinates to find the limit:

$$\lim_{(x,y)\to(0,0)} \frac{e^{-x^2-y^2}-1}{x^2+y^2}.$$

**2.** (9 points) Use implicit differentiation to find  $\partial z/\partial x$  and  $\partial z/\partial y$  if

$$e^z = xyz.$$

**3.** (8 points) Find an equation for the tangent plane to the surface  $z = e^{x-y}$  at the point (2, 2, 1). Write the equation in the form z = ax + by + d.

4. (8 points) Given that f(x, y) is a differentiable function with

f(2,5) = 6,  $f_x(2,5) = 1$ ,  $f_y(2,5) = -1$ ,

use a linear approximation to estimate f(2.2, 4.9).

**5.** (9 points) If

 $w = xe^{y/z}, \quad x = t^2, \quad y = 1 - t, \quad z = 1 + 2t,$ 

find  $\partial w/\partial t$  at the point where t = 0.

6. (9 points) Find the directional derivative of the function  $f(x, y, z) = x^2y + y^2z$  at the point (1, 2, 3) in the direction of the vector  $\mathbf{v} = \langle 2, -1, 2 \rangle$ .

7. (9 points) Find the maximal rate of change of  $f(x, y) = 4y\sqrt{x}$  at the point (4, 1) and the direction in which it occurs.

8. (9 points) Find the parametric equations for the normal line to the ellipsoid

$$\frac{x^2}{4} + y^2 + \frac{z^2}{9} = 3$$

at the point (-2, 1, -3).

9. (10 points) Find the critical points of  $f(x, y) = x^4 - 2x^2 + y^3 - 3y$  and classify them as local maximum, local minimum, or saddle point.

10. (10 points) Find the absolute maximum and minimum values of

$$f(x,y) = x + \sqrt{3}y$$

on the unit disk

$$D = \left\{ (x,y) \mid x^2 + y^2 \le 1 \right\}$$

and the points of D where these values are reached.

11. (11 points) Use Lagrange multipliers to find the extreme values of

$$f(x, y, z) = xy^2 z$$

subject to the constraint

$$x^2 + y^2 + z^2 = 4.$$

[*Note*: No credit will be given if a different method is used.]