MA 213 - Calculus III
Fall 2017
Final Exam December 11, 2017

## Exam Scores

Do not write in the table below

Name: $\qquad$

Section: $\qquad$

Last 4 digits of student ID \#: $\qquad$

- No books or notes may be used.
- Turn off all your electronic devices and do not wear ear-plugs during the exam.
- You may use a calculator, but not one which has symbolic manipulation capabilities or a QWERTY keyboard.
- All questions are free response questions. Show all your work on the page of the problem. Clearly indicate your answer and the reasoning used to arrive at that answer. Unsupported answers may not receive credit.

| Question | Score | Total |
| :---: | ---: | ---: |
| 1 |  | 9 |
| 2 |  | 9 |
| 3 |  | 9 |
| 4 |  | 9 |
| 5 |  | 9 |
| 6 |  | 9 |
| 7 |  | 9 |
| 8 |  | 10 |
| 9 |  | 9 |
| 10 |  | 9 |
| 11 |  | 9 |
| Total |  | 100 |

## Free Response. Show your work!

1. (9 points) Find an equation for the plane through the points $(0,1,1),(1,0,1)$, and $(1,1,0)$.
2. (9 points) Find the acute angle between the lines $2 x-y=3$ and $3 x+y=7$ in the $x y$-plane.

## Free Response. Show your work!

3. (9 points) Find the curvature of the plane curve $y=x e^{x}$ at the point $(0,0)$.
4. (9 points) Find an equation for the tangent plane to the surface $z=x \sin (x+y)$ at the point $(-1,1,0)$. Write the equation in the form $x+b y+c z=d$.

## Free Response. Show your work!

5. (9 points) Use implicit differentiation to find $\partial z / \partial x$ and $\partial z / \partial y$ if

$$
x^{2}+2 y^{2}+3 z^{2}=1 .
$$

6. (9 points) Find all the points on the line $x=3$ at which the direction of fastest change of the function $f(x, y)=x^{2}+y^{2}-2 x-4 y$ is $\mathbf{i}+\mathbf{j}$.

## Free Response. Show your work!

7. (9 points) Find the critical points of $f(x, y)=x^{2}+y^{4}+2 x y$ and classify them as local maximum, local minimum, or saddle point.

## Free Response. Show your work!

8. (10 points) Use spherical coordinates $(\rho, \theta, \phi)$ to find the volume of the part of the ball $\rho \leq 3$ that lies between the cones $\phi=\pi / 6$ and $\phi=\pi / 3$.
9. (9 points) Evaluate

$$
\int_{C} x y^{4} d s
$$

where $C$ is the right half of the circle $x^{2}+y^{2}=4$.

## Free Response. Show your work!

10. (9 points) Let $\mathbf{F}(x, y)=\left\langle 2 x e^{-y}, 2 y-x^{2} e^{-y}\right\rangle$. Find a potential function for $\mathbf{F}(x, y)$ and evaluate

$$
\int_{C} \mathbf{F} \cdot d \mathbf{r}
$$

where $C$ is any path from $(1,0)$ to $(2,1)$.
11. (9 points) Use Green's Theorem to evaluate

$$
\int_{C} y^{3} d x-x^{3} d y
$$

where $C$ is the positively oriented circle $x^{2}+y^{2}=4$.

