Quiz 1 Solution

- 1. Find the following integrals.
 - (a) (5 points) $\int x^2(\ln x) dx$

Solution: Let $u = \ln x$ and $dv = x^2 dx$. Then, $du = \frac{dx}{x}$ and $v = \frac{x^3}{3}$. So, the integral becomes

$$\int x^2(\ln x)dx = uv - \int vdu = \frac{x^3}{3}\ln x - \int \frac{x^2}{3}dx = \frac{x^3}{3}\ln x - \frac{x^3}{9} + C$$

(b) (5 points) $\int t^3 \sin(t^2) dt$ Solution: Let $s = t^2$. Then, ds = 2tdt, so

$$\frac{1}{2}\int s\sin(s)ds$$

Now, we do integration by parts. Let u = s and $dv = \sin s ds$. Then, du = ds and $v = -\cos s$. So, the integral becomes

$$\frac{1}{2}\int s\sin sds = \frac{1}{2}\left[-s\cos s + \int \cos s \, ds\right] = \frac{1}{2}\left[-t^2\cos(t^2) + \sin(t^2)\right] + C$$