

Answer all questions and show your work. Unsupported answers may receive *no credit*. You may not use a calculator on this quiz. Allow 15 minutes for the quiz.

Name: \_\_\_\_\_ Section: \_\_\_\_\_

1. (5 points) Let  $R$  be the region in the first quadrant bounded by the functions  $y = x^2$ ,  $y = 6 - x$ , and  $x = 0$  (the  $y$ -axis). Set up but *do not evaluate* the integral that calculates the volume of the solid obtained by rotating  $R$  about the  $y$ -axis using the Shell Method.

**Solution:**

The points of intersection are  $x = -3$  and  $x = 2$  obtained by solving  $x^2 = 6 - x$  but only  $x = 2$  is in the first quadrant. Since the regions is bounded by  $y = x^2$ ,  $y = 6 - x$  and  $x = 0$ , using the Shell Method,

$$V = 2\pi \int_0^2 x(6 - x - x^2)dx$$

2. (5 points) Let  $S$  be a surface obtained by rotating  $y = x^4$  from  $(1, 1)$  to  $(2, 16)$  around the  $x$ -axis. Set up but *do not evaluate* the integral that calculates the surface area of  $S$ .

**Solution:**

Note that for  $y = f(x)$ , the derivative is  $y' = 4x^3$  then by the formula for the surface area of the revolution,

$$V = 2\pi \int_1^2 x^4 \sqrt{1 + (4x^3)^2} dx$$