#### Lecture on sections 1.1,1.2

#### Ma 162 Spring 2010

Ma 162 Spring 2010

January 13, 2010

Avinash Sathaye (Ma 162 Spring 2010 Beginning of Coordinate Geometry

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- A linear function of one variable x is a function f(x) = mx + c where m, c are constants. Its graph is a straight line, hence it is called linear.
  Example: f(x) = 3x + 4.
  - For the function of two variables x, y is of the form f(x, y) = ax + by + c. Its graph is a plane in three space. **Example:** f(x, y) = 3x + 4y + 5.
    - A natural generalization is a linear function of n variables  $f(x_1, x_2, \cdots, x_n) = -a_1 x_1 + a_2 x_2 + \cdots + a_n x_n + b$  where

    - Example: f(x, y, z) = 3z + 4y 5z + 7.
    - These functions are useful in many applications.
    - What are examples of functions which are not linear? Example:

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   Example:
   f(x) = x<sup>2</sup> + 3x, q(x, y) = x<sup>3</sup> y<sup>3</sup>, h(x, y, z) = xy + yz + zx.

- **Distance traveled** If the time interval is short or if an object is moving without acceleration, then *s* = *at* + *b* describes the distance traveled at time *t*. The coefficient *a* is the constant **velocity**. Its sign describes if the object is moving away or coming closer.
- Revenue, Cost and Profit Function. If x is the number of units sold or manufactured, then we have three natural functions associated with it.
- The cost function is G(x) = cx + f where c is the production cost per unit and f is the fixed cost.
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Here are some examples of real life functions which behave like linear functions.

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- The profit function: P(x) = R(x) C(x) or (p-c)x f.

We now review how to study the properties of a linear function of one variable x by known geometric properties of its graph, the line.

- Plane coordinates Recall that points in the plane are pairs of numbers (x, y), these are the x and y coordinates respectively.
  - A point named P with coordinates (2,3) can be denoted as P(2,3).
- **Distance Formula.** Recall that the distance between two points  $P(a_1, b_1)$  and  $Q(a_2, b_2)$  is given by the formula

$$d(P, Q) = \sqrt{(a_2 - a_1)^2 + (b_2 - b_1)^2}.$$

**Example.** The distance between P(2,3), Q(-1,7) is:

#### $d(P, Q) = \sqrt{(-1-2)^2 + (7-3)^2} = \sqrt{9+16} = 5.$

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## Graph of a function.

The graph of a function y = f(x) consists of all points P(x, y) for which y = f(x). Example. The graphs of the lines

$$y = \frac{2x}{3}, y = 1 - \frac{2x}{3}$$
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## More about lines

- As the graph of a linear function, a line has the equation y = mx + c.
- A vertical line does not appear as the graph of linear function. Indeed, it cannot be the graph of **any function**. A vertical line is described by an equation of the form x = p where p is a constant.
- We may combine these two cases and say that the general equation of a line in the plane is of the form:

ax + by + c = 0

where at least one of a, b is non zero.

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• Given a line ax + by + c = 0, if  $b \neq 0$ , then it is not vertical. <Indeed,> we can rewrite it as

$$by = -ax - c$$
 or  $y = \frac{-a}{b}x + \frac{-c}{b}$ .

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Example

The line 2x - 3y + 5 = 0 is rewritten as  $y = \frac{-2}{2}x + \frac{-5}{2}$  or

- $y = \frac{2}{3}x + \frac{5}{3}.$
- The slope of the general line ax + by + c = 0 is  $m = -\frac{a}{b}$  when  $b \neq 0$ .

If b = 0 then the line is vertical and slope is infinite. We sometimes allow an equation  $m = \infty$  to express this idea.

• Positive slope describes a line rising to the right, negative slope describes a line falling to the right, zero slope gives a horizontal line.



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Given two distinct points in the plane, there is a unique line joining them.
If the two points are (a<sub>1</sub>, b<sub>1</sub>) and (a<sub>2</sub>, b<sub>2</sub>), then the slope of this line is:

$$m = \frac{b_2 - b_1}{a_2 - a_1}.$$

**Example:** The slope of the line joining (2,3) and (-1,6) is:

Formula for Slope

$$\frac{6-3}{-1-2} = -1.$$

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#### More Equations of Lines.

• The equation of a line with a given slope m and passing through a point (a, b) is:

**Point Slope Formula**. y - b = m(x - a)

**Example:** The slope of the line joining (2,3) and (-1,6) is already calculated to be -1. Using it and the point (2,3), we get:

y-3 = -1(x-2) simplifies to y = -x+5 or x+y-5 = 0.

• As expected, all formulas need a special handling when the slope becomes infinite, i.e. when the line is vertical. The reader should make this adjustment as necessary.

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- The intercept of a line refers to its intersection with an axis, when defined.
- Thus, the x-intercept of a line ax + by + c = 0 is given by its intersection with the x-axis (i.e. y = 0) and is clearly equal to  $-\frac{c}{-}$ .
  - When a = 0, this is infinite if  $c \neq 0$  and undefined when c = 0, i.e. when the line is the whole x-axis.
- Similarly, the *y*-intercept of a line ax + by + c = 0 is given by its intersection with the *y*-axis (i.e. x = 0) and is clearly equal to  $-\frac{c}{L}$ .
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- Note that for the line equation y = mx + c, the y-intercept is c.

- Example: What are the x and y intercepts of 2x 3y + 5 = 0?
  - **Answer:** The *x*-intercept is  $-\frac{5}{2}$  and the *y*-intercept is  $\frac{5}{3}$ .
- Sometimes, it is desirable to get the equation of a line with given x-intercept p and y-intercept q.
   A nice formula is:
  - Intercept Form.

$$\frac{x}{p} + \frac{y}{q} = 1$$

**Example:** What is the equations of a line with x-intercept -3 and y-intercept 2? Answer:

 $\frac{x}{-3} + \frac{y}{2} = 1$  which simplifies to 2x - 3y + 6 = 0.  $\frac{x}{-3} + \frac{y}{2} = 1$  which simplifies to 2x - 3y + 6 = 0.

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