

Quiz #8

Directions: Carefully read each question below and answer to the best of your ability in the space provided. Your answer to problems should be written in a clear and concise manner.

You **MUST** show your work to receive full credit!

1. (5 points) Find the images of $\vec{u} = \begin{bmatrix} 5 \\ -2 \end{bmatrix}$ and $\vec{v} = \begin{bmatrix} 1 \\ 3 \end{bmatrix}$ under the linear transformation $T : \mathbb{R}^2 \rightarrow \mathbb{R}^2$, defined by $T(\vec{x}) = A\vec{x}$ with $A = \begin{bmatrix} 2 & 1 \\ 3 & -2 \end{bmatrix}$.

2. (5 points) For the following linear transformations find the corresponding 2×2 matrix.

1. Dilation by a factor of 3
2. Rotation by 45-degrees clockwise
3. Identity matrix
4. Rotation by 60-degrees counterclockwise
5. Projection onto the x -axis

Hint: Recall that a general form of the rotation matrix R_α is

$$R_\alpha = \begin{bmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{bmatrix}$$

where $\alpha > 0$ would correspond to the rotation counterclockwise.

Name: _____

Section (circle one): 001 002

| | | | |
|-----------|---|---|-------|
| Question: | 1 | 2 | Total |
| Points: | 5 | 5 | 10 |
| Score: | | | |