

1. Find the definite integrals using the fundamental theorem of calculus. You may need to use a substitution.

a. $\int_0^x e^t dt$

b. $\int_0^x (t+3)^2 dt$

c. $\int_0^x \sqrt{t+9} dt$

d. $\int_0^x \frac{3}{(4t+5)} dt$

e. $\int_0^x 6e^{3t-2} dt$

f. $\int_0^x 3t^2 e^{t^3+2} dt$

2. Consider the function $F(x) = \int_{-2}^x \frac{1}{1+t^2} dt$.

Determine the intervals on which $F(x)$ is increasing.

3. Find the average value of $g(x) = e^{2x}$ on the interval $[1, 4]$.

4. A rock is dropped from a cliff. The velocity of the rock, measured in feet per second, after t seconds, is $v(t) = -32t$. The rock hits the ground 10 seconds later. How high is the cliff?