

**MA 614 – Homework 21**  
**Due Friday, March 11**

Your answers should be detailed explanations in quality mathematical English. You must type your homework in LaTeX.

1. Let  $a_n$  be the number of ways of doing the following: Partition the elements of  $[n]$  into nonempty blocks, then partition the blocks themselves into nonempty “superblocks.”
  - (a) Determine the egf for  $a_n$ .
  - (b) Calculate  $a_3$  and confirm this value by explicitly enumerating all possibilities.
2. Find the egf and an expression for the number of permutations of  $[n]$  having no 2-cycles.
3. Suppose we have a room with  $n$  children which are distinguishable. The children gather into circles by holding hands, and one child stands in the center of each circle. A circle may consist of as few as one child clasping his or her hands around the other child at the center of the circle. Let  $h_n$  be the number of ways this can be done. Find the egf for  $h_n$ .