

**MA 614 – Homework 4**  
**Due Monday, Jan 24**

Your answers should be detailed explanations in quality mathematical English. You must type your homework in LaTeX.

1. Let  $n \in \mathbb{P}$  and consider a  $1 \times n$  chessboard  $X_n$  (i.e., a chessboard that has one horizontal row of  $n$  squares). Determine the number  $t_n$  of ways to tile  $X_n$  with the following types of tiles: red, blue and green  $1 \times 1$  tiles; yellow and orange  $1 \times 4$  tiles; and black and white  $1 \times 5$  tiles.
2. Give a bijection between compositions of  $n$  into 1's and 2's and compositions of  $n + 1$  into odd parts.
3. Give a bijective proof of the identity

$$\binom{\binom{n}{2}}{2} = 3\binom{n}{4} + n\binom{n-1}{2}.$$