

1. Find the Laplace transform of $\int_0^t (t-w)^2 \cos 2w \, dw$.

Hint: use the fact that $L(f * g) = F(s)G(s)$.

2. Find the inverse Laplace transform of each expression. Your answers should include an integral.

a. $\frac{s}{(s+1)(s^2+4)}$

b. $\frac{G(s)}{s^2+16}$

3. Use Laplace transforms to solve the initial value problem
 $y'' + 4y' + 4y = g(t); \quad y(0) = 2, \quad y'(0) = -3.$