

**MA681–001 Functional Analysis**  
**Fall 2013**  
**Problem Set 2**  
**DUE: Wednesday, 18 September 2013**

1. Complete the proof of Proposition A3.9 on page 303 of Hislop & Sigal. This is problem A3.3. You should think about why the extension is well-defined and unique.
2. Read pages 305–306 on the set of all bounded operators from  $X$  to  $Y$ , which is denoted  $\mathcal{L}(X, Y)$ . Do problem A3.7, which finishes the proof that this algebra is a Banach space. When we have  $X = Y$ , show that  $\mathcal{L}(X)$  is a Banach algebra.
3. Problems 1.3 and 1.4 on page 15.