MA111: Contemporary mathematics

Jack Schmidt

University of Kentucky

November 12, 2012

Entrance Slip (due 5 min past the hour):

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Today we investigate last diminisher.

Exam and HW is Nov 19.

Context: How to make a pile file

- Suppose a judge tries to tell the players that a pile is "fair"
- Some players think it is too small, some think it is too big, some think it is just right
- Which player should get the pile?
- If a player thinks it is too small, he will be mad if he gets it
- Just right: won't care either way
- Too big: will be made if someone else gets it
- So if two people think it is too big, then the judge has ruined it!

Activity: Last diminisher

We'll play last diminisher in front of the class

We'll cover the "sandwich" model

Make sure you understand how to play

Make sure you understand how to protect yourself against cheaters!

Fast: Last diminisher

- Requirements: Any number N of players; loot that can be divided arbitrarily and recombined without loss of value
- Overview: Each player one player (the least greedy) will leave "happy"
- Rules:
 - Randomly order the remaining players. The initial piece is the whole loot.
 - In order, each player declares the pile too small, just right, or too big.
 - 3 If too big: they also make the pile smaller until they declare it is just right.
 - 4 After everyone is done, the last player who didn't say too small gets the pile.
 - Sepeat until everyone has left
- ▶ 1 is important, because the very last player has an advantage

Fast: strategy for everyone but last

- Be honest!
- If it is too small, say so, so you won't get stuck with it
- If it is just right, you can say "too small" without any real harm to yourself, but you'll have to wait until next round
- If it is too big, you need to say so to prevent the next player from taking more than his fair share
- Sad part: you can only get exactly your fair share.

Fast: strategy for the last player

• Only change: If it is too big, take it!

• There is no "next player" to worry about

• If you are greedy and patient, you can reject "just right" pieces

Assignment and exit slip

- Read and understand 3.1-3.5. Skim 3.6.
- Homework due Nov 19.
- Exit slip: You are third player in Last diminisher

There are five players

The current pile is 40% of the loot

 What percentage of the loot should you make the pile? [Or should you just say "too small" and pass?]