MA162: Finite mathematics

Jack Schmidt

University of Kentucky

August 27, 2012

SCHEDULE:

- HW 0.2 is due Thursday, Aug 30th, 2012.
- HW 1.1-1.4 are due Friday, Aug 31st, 2012.
- HW 2.1-2.2 are due Friday, Sep 7th, 2012.
- Exam 1 is Monday, Sep 24th, 5:00pm-7:00pm in BS107 and BS116.

Today we will cover 1.3 and 1.4: cost/revenue/profit and supply/demand.

- You can sell corn at \$17 per bushel
- It costs you \$4 per bushel to make it
- Before you even make a single bushel of corn, you are \$1001 in debt
- How much are you in debt to make 10 bushels?
- How much do you sell those 10 bushels for?
- How does that work out for you?

Well your costs are easy: \$1001 plus \$4 per bushel

$$C(x) = 1001 + 4x$$

Your revenue is easy: \$17 per bushel

$$R(x) = 17x$$

 So profit is easy, you start \$1001 in the hole, and make \$13 per bushel

$$P(x) = -1001 + 13x$$

- At 10 bushels, you've made \$170 but spent \$1041, so you are \$871 in debt
- At 20 bushels, you've made \$340 but spent \$1081, so you are \$741 in debt
- Every additional 10 bushels gets you an additional \$130 closer to breaking even
- \$741/\$130 is about 5.7 so probably need another 57 bushels, let's check:
- At 77 bushels, you've made \$1309 but spent \$1309, so you've just broken even
- \bullet At 100 bushels, you've made \$1700 but spent \$1401, so you are \$299 ahead
- (100-77)(13) = (23)(13) = 299. Not a coincidence.

• Marginal cost is \$4 per bushel

- Fixed cost is \$1001
- Marginal revenue is \$17 per bushel
- Marginal revenue is \$13 per bushel
- Break-even production is 77 bushels

- Fixed and marginal cost (new product)
- 20 cost \$200, 25 cost \$220, how much do 30 cost?

(Left) \$300

(Right) \$240

(Both) \$225

- Fixed and marginal cost (new product)
- 20 cost \$200, 25 cost \$220, how much do 30 cost?

```
(Left) $300
```

(Right) \$240

(Both) \$225

Discuss with your neighbors, because you'll explain it to us next

- Fixed and marginal cost (new product)
- 20 cost \$200, 25 cost \$220, how much do 30 cost?

```
(Left) $300
```

(Right) \$240

(Both) \$225

- Discuss with your neighbors, because you'll explain it to us next
- Now explain it to us, especially someone who changed their mind.

• 20 cost \$200, 25 cost \$220, how much do 30 cost?

(Left) \$300 – This assumes each one costs \$10, but then 25 should have costed \$250

(Right) \$240 – 5 more costed \$20 more, so another 5 costs another \$20

(Both) 5 more costs \$5 more? Life isn't that simple

- 20 cost \$200, 25 cost \$220, how much do 30 cost?
- (Left) \$300 This assumes each one costs \$10, but then 25 should have costed \$250
- (Right) \$240 5 more costed \$20 more, so another 5 costs another \$20
 - (Both) 5 more costs \$5 more? Life isn't that simple
 - So Marginal cost is \$20 per 5, or \$4 each

- 20 cost \$200, 25 cost \$220, how much do 30 cost?
- (Left) \$300 This assumes each one costs \$10, but then 25 should have costed \$250
- (Right) \$240 5 more costed \$20 more, so another 5 costs another \$20
 - (Both) 5 more costs \$5 more? Life isn't that simple
 - So Marginal cost is \$20 per 5, or \$4 each
 - So fixed cost is \$120

```
    50 cost $500, 100 cost $700, how much do 75 cost?
    (Left) $750
    (Right) $900
    (Both) $600
```

50 cost \$500, 100 cost \$700, how much do 75 cost?
 (Left) \$750
 (Right) \$900
 (Both) \$600

 50 more cost \$200 more, so 25 more only costs \$100 more (Both) \$600

• 50 cost \$500, 100 cost \$700, how much do 75 cost?

(Left) \$750

(Right) \$900

(Both) \$600

- 50 more cost \$200 more, so 25 more only costs \$100 more (Both) \$600
- Marginal cost is \$4 each

50 cost \$500, 100 cost \$700, how much do 75 cost?
 (Left) \$750
 (Right) \$900
 (Both) \$600

- 50 more cost \$200 more, so 25 more only costs \$100 more (Both) \$600
- Marginal cost is \$4 each
- Fixed cost is \$300, since \$4 each for 50 is only \$200, not \$500

Ch 1.4: Intersecting lines: Examples 2-5

The break-even point is when the revenue equals the cost

$$P(x) = C(x)$$

• To solve 17x = 1001 + 4x, move the xs over to get

$$13x = 1001$$
 $x = 1001/13 = 77$

- A pessimistic phrasing is when the profit is zero
- P(x) = 0
- To solve -1001 + 13x = 0, move the 1001 over to get

$$13x = 1001$$
 $x = 1001/13 = 77$

Ch 1.3: Example 3: Supply function

- All else being equal, more people are willing to supply at a higher price
- x = 40p + 100 describes the number x of bushels people are willing to supply at a price p in dollars per bushel.

 The 40 has units "bushels per (dollar per bushel)" and the 100 has units "bushels"
- How many bushels would be supplied at \$4 per bushel?
- How many bushels would be supplied at \$5 per bushel?
- How many bushels would be supplied at \$17 per bushel?
- How many extra bushels are supplied for every extra dollar per bushel in price?

Ch 1.3: Example 3: Demand function

- Demand is exactly the same, but is controlled by the buyers.
- The demand is 1170 bushels at \$4 per bushel
- The demand drops to 0 bushels at \$17 per bushel
- In the middle, we assume a "linear demand curve" or model
- How much did the demand drop?
- How much did the price increase?
- How much did demand drop per dollar of price increase?
- What would the demand at \$5 per bushel be?

Ch 1.4: Example 6-7: Market equilibrium

• How much is supplied at \$4 per bushel? How much is demanded? What is the shortfall?

• How about at \$5? What is the shortfall?

• How much does the shortfall decrease per dollar-per-bushel increase in price?

• When does the shortfall drop to 0?

Ch 1.4: Worked out

- At \$4, we calculated supply 260 bushels, demand was 1170 bushels, shortfall is 910
- At \$5, we calculated supply was 300 bushels, demand was 1080, shortfall is 780
- Each dollar the supply increases by 40 and the demand drops by 90, so the shortfall is dropping by 40 + 90 = 130 bushels
- At \$4 the shortfall is 910, so we need to raise the price by another 910/130=7 dollars per bushel to drop the shortfall to 0
- ullet That is \$4 + \$7 = \$11 per bushel at market equilibrium

Ch 1.4: Example 6-7: Market equilibrium

- In a rational, free market, the demand (number of items bought) equals the supply (number of items sold)
- On the exam, a problem like this requires you to:
 - find the supply equation
 - find the demand equation
 - set them equal to each other
 - solve for the equilibrium quantity
 - substitute back in for the equilibrium price (or vice versa)

Ch 1.3 and 1.4 summary

- Concentrate on how the slope answers most of these questions with bunny hops
- There are also tax and temperature questions in the textbook
- The homework and exams will use words like: linear depreciation, cost function, revenue function, profit function, fixed costs, variable costs, supply equation, demand equation, market equilibrium
- Homework is due Friday, 1.1-1.4
- I am heading to the mathskeller now for a bit, and will be there from 2pm to 4pm this afternoon