MA162 2013-03-25 Ch 6.1: Sets

1. If one can borrow a car every Monday, Tuesday, Wednesday, and every Tuesday, Thursday, and Friday, then how many days can one borrow the car per week?

- 2. Which of the sets are equal?
 - $\{1,2,3\} \stackrel{?}{=} \{1,2,3\}$
 - $\{1,2,3\} \stackrel{?}{=} \{1,2\}$
 - $\{1,2,3\} \stackrel{?}{=} \{3,1,2\}$
 - $\{1,2,3\} \stackrel{?}{=} \{1,2,2,3,3,3\}$
 - $\{1,2,3\} \stackrel{?}{=} \{$ positive integers whose square has one digit $\}$
 - $\{1,2,3\} \stackrel{?}{=} \{ \text{ odd numbers less than } 4 \}$
- 3. Calculate the following unions and intersections:
 - $\{1,2,3\} \cup \{3,4,5\} =$
 - $\{1,2,3\} \cap \{3,4,5\} =$
 - $\{1,2,3\} \cup \{1\} =$
 - $\{1,2,3\} \cap \{1\} =$
- 4. Calculate the following differences:
 - $\{1,2,3\} \{1\} =$
 - $\{1,2,3\} \{2,3\} =$
 - $\{1,2,3\} \{3,4,5\} =$
 - $\{1,2,3\} \{4,5,6\} =$
 - $\{1,2,3\} \{1,2,3\} =$
- 5. Simplify the following expressions:
 - $(A \cap (B \cup C)) ((A \cap B) \cup (A \cap C)) =$
 - A A =
 - \bullet $A \cap A =$
 - \bullet $A \cup A =$
 - $\bullet \ (A \cup A) A =$
 - \bullet $A \cup (A A) =$

6. A standard 52-card deck of playing cards has the following cards: $\mathsf{A} \heartsuit \ 2 \heartsuit \ 3 \heartsuit \ 4 \heartsuit \ 5 \heartsuit \ 6 \heartsuit \ 7 \heartsuit \ 8 \heartsuit \ 9 \heartsuit \ 10 \heartsuit \ \mathsf{J} \heartsuit \ \mathsf{Q} \heartsuit \ \mathsf{K} \heartsuit$ $A \diamondsuit 2 \diamondsuit 3 \diamondsuit 4 \diamondsuit 5 \diamondsuit 6 \diamondsuit 7 \diamondsuit 8 \diamondsuit 9 \diamondsuit 10 \diamondsuit J \diamondsuit Q \diamondsuit K \diamondsuit$ A\$ 2\$ 3\$ 4\$ 5\$ 6\$ 7\$ 8\$ 9\$ 10\$ J\$ Q\$ K\$ A\$\dagger\$ 2\$\dagger\$ 3\$\dagger\$ 4\$\dagger\$ 5\$\dagger\$ 6\$\dagger\$ 7\$\dagger\$ 8\$\dagger\$ 9\$\dagger\$ 10\$\dagger\$ J\$\dagger\$ Q\$\dagger\$ K\$\dagger\$ If 5 people are playing, and each has been dealt 10 cards, then: (a) Why must one of the suits $(\heartsuit, \diamondsuit, \clubsuit, \spadesuit)$ be completely dealt out? (b) Must at least two people have at least one clubs ♣? (c) Must at least one person has at least two clubs \\$? (d) Must every player have at least 3 of the same suit?

(e) Must some pair of neighbors have at least 6 of the same suit combined (it counts, even if one player has 6 all by themselves)