Probability Worksheet #6 October 5, 2018 2 Points

Circ	ما	ono	nan	20

Name:	Name:	Name:

Note:
$$P(E|F) = \frac{\text{size of } E \cap F}{\text{size of } F}$$
.

Note: Two events E and F are said to be independent if P(F|E) = P(F).

1. A deck of 10 cards has 2 suits (A-B) and 5 ranks (1-5).

Suit \ Rank	1	2	3	4	5
A	A1	A2	A3	A4	A5
В	B1	B2	В3	B4	В5

Let E be the event "A card with suit B is drawn."

Let F be the event "A card with rank 2 is drawn."

(a)
$$P(E) = ?$$

(b)
$$P(F) = ?$$

(c)
$$P(E \cap F) = ?$$

(d)
$$P(E \cup F) = ?$$

(e)
$$P(E|F) = ?$$

(f)
$$P(F|E) = ?$$

- (g) Are the events E and F independent in this example? How do you know?
- (h) Does $P(E) \cdot P(F) = P(E \cap F)$ in this example?

2. A deck of 8 cards has 2 suits and 5 ranks, but cards B4 and B5 are not included:

Suit \ Rank	1	2	3	4	5
A	A1	A2	A3	A4	A5
В	B1	B2	В3		

Let E be the event "A card with suit B is drawn." Let F be the event "A card with rank 2 is drawn."

(a)
$$P(E) = ?$$

(b)
$$P(F) = ?$$

(c)
$$P(E \cap F) = ?$$

(d)
$$P(E \cup F) = ?$$

(e)
$$P(E|F) = ?$$

(f)
$$P(F|E) = ?$$

- (g) Are the events E and F independent in this example? How do you know?
- (h) Does $P(E) \cdot P(F) = P(E \cap F)$ in this example?
- 3. In a standard deck of 52 cards there are four suits and 13 ranks.
 - (a) Suppose a card is drawn from the deck at random, and it turns out to be the ace of spades. Suppose the ace of spades is returned to the deck ("with replacement"), and again a card is drawn at random. What is the probability that it is a spade?
 - (b) Suppose a card is drawn from the deck at random, and it turns out to be the ace of spades. Suppose the ace of spades is NOT returned to the deck ("without replacement"), and a second card is drawn at random. What is the probability that it is a spade?