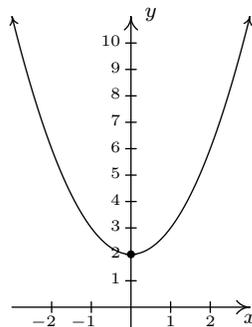
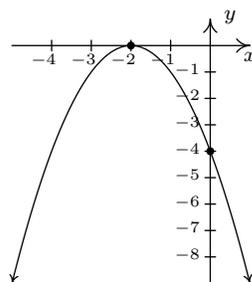


Worksheet 6 KEY - Quadratic Functions (§4.1)

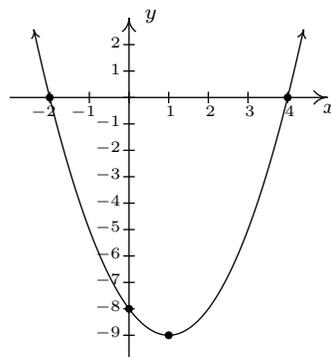
1. $f(x) = x^2 + 2$ (this is both forms!)

No x -intercepts y -intercept $(0, 2)$ Domain: $(-\infty, \infty)$ Range: $[2, \infty)$ Decreasing on $(-\infty, 0]$ Increasing on $[0, \infty)$ Vertex $(0, 2)$ is a minimumAxis of symmetry $x = 0$ 

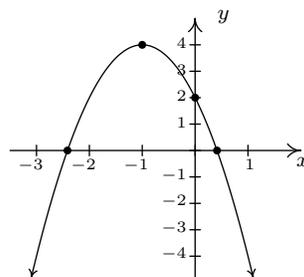
2. $f(x) = -(x + 2)^2 = -x^2 - 4x - 4$

 x -intercept $(-2, 0)$ y -intercept $(0, -4)$ Domain: $(-\infty, \infty)$ Range: $(-\infty, 0]$ Increasing on $(-\infty, -2]$ Decreasing on $[-2, \infty)$ Vertex $(-2, 0)$ is a maximumAxis of symmetry $x = -2$ 

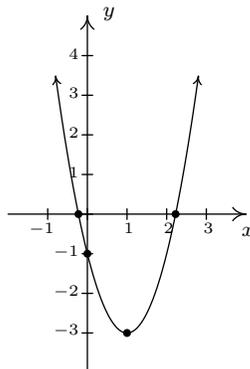
3. $f(x) = x^2 - 2x - 8 = (x - 1)^2 - 9$

 x -intercepts $(-2, 0)$ and $(4, 0)$ y -intercept $(0, -8)$ Domain: $(-\infty, \infty)$ Range: $[-9, \infty)$ Decreasing on $(-\infty, 1]$ Increasing on $[1, \infty)$ Vertex $(1, -9)$ is a minimumAxis of symmetry $x = 1$ 

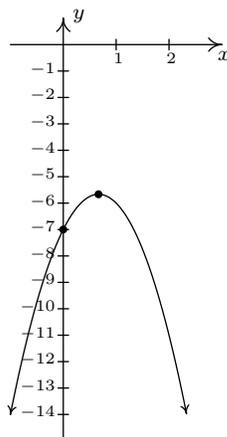
4. $f(x) = -2(x + 1)^2 + 4 = -2x^2 - 4x + 2$

 x -intercepts $(-1 - \sqrt{2}, 0)$ and $(-1 + \sqrt{2}, 0)$ y -intercept $(0, 2)$ Domain: $(-\infty, \infty)$ Range: $(-\infty, 4]$ Increasing on $(-\infty, -1]$ Decreasing on $[-1, \infty)$ Vertex $(-1, 4)$ is a maximumAxis of symmetry $x = -1$ 

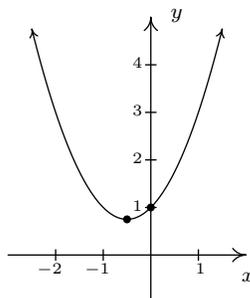
5. $f(x) = 2x^2 - 4x - 1 = 2(x - 1)^2 - 3$
 x -intercepts $\left(\frac{2-\sqrt{6}}{2}, 0\right)$ and $\left(\frac{2+\sqrt{6}}{2}, 0\right)$
 y -intercept $(0, -1)$
 Domain: $(-\infty, \infty)$
 Range: $[-3, \infty)$
 Increasing on $[1, \infty)$
 Decreasing on $(-\infty, 1]$
 Vertex $(1, -3)$ is a minimum
 Axis of symmetry $x = 1$



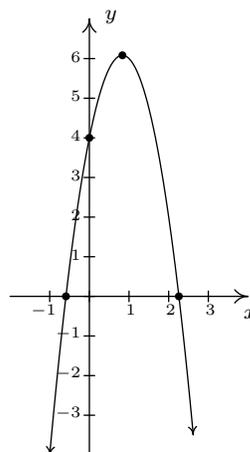
6. $f(x) = -3x^2 + 4x - 7 = -3\left(x - \frac{2}{3}\right)^2 - \frac{17}{3}$
 No x -intercepts
 y -intercept $(0, -7)$
 Domain: $(-\infty, \infty)$
 Range: $(-\infty, -\frac{17}{3}]$
 Increasing on $(-\infty, \frac{2}{3}]$
 Decreasing on $[\frac{2}{3}, \infty)$
 Vertex $(\frac{2}{3}, -\frac{17}{3})$ is a maximum
 Axis of symmetry $x = \frac{2}{3}$



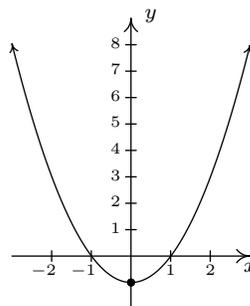
7. $f(x) = x^2 + x + 1 = \left(x + \frac{1}{2}\right)^2 + \frac{3}{4}$
 No x -intercepts
 y -intercept $(0, 1)$
 Domain: $(-\infty, \infty)$
 Range: $[\frac{3}{4}, \infty)$
 Increasing on $[-\frac{1}{2}, \infty)$
 Decreasing on $(-\infty, -\frac{1}{2}]$
 Vertex $(-\frac{1}{2}, \frac{3}{4})$ is a minimum
 Axis of symmetry $x = -\frac{1}{2}$



8. $f(x) = -3x^2 + 5x + 4 = -3\left(x - \frac{5}{6}\right)^2 + \frac{73}{12}$
 x -intercepts $\left(\frac{5-\sqrt{73}}{6}, 0\right)$ and $\left(\frac{5+\sqrt{73}}{6}, 0\right)$
 y -intercept $(0, 4)$
 Domain: $(-\infty, \infty)$
 Range: $(-\infty, \frac{73}{12}]$
 Increasing on $(-\infty, \frac{5}{6}]$
 Decreasing on $[\frac{5}{6}, \infty)$
 Vertex $(\frac{5}{6}, \frac{73}{12})$ is a maximum
 Axis of symmetry $x = \frac{5}{6}$



9. $f(x) = x^2 - \frac{1}{100}x - 1 = \left(x - \frac{1}{200}\right)^2 - \frac{40001}{40000}$
 x -intercepts $\left(\frac{1+\sqrt{40001}}{200}, 0\right)$ and $\left(\frac{1-\sqrt{40001}}{200}, 0\right)$
 y -intercept $(0, -1)$
 Domain: $(-\infty, \infty)$
 Range: $[-\frac{40001}{40000}, \infty)$
 Decreasing on $(-\infty, \frac{1}{200}]$
 Increasing on $[\frac{1}{200}, \infty)$
 Vertex $(\frac{1}{200}, -\frac{40001}{40000})$ is a minimum
 Axis of symmetry $x = \frac{1}{200}$



10. The vertex is (approximately) $(29.60, 22.66)$, which corresponds to a maximum fuel economy of 22.66 miles per gallon, reached sometime between 2009 and 2010 (29 – 30 years after 1980.) Unfortunately, the model is only valid up until 2008 (28 years after 1908.) So, at this point, we are using the model to *predict* the maximum fuel economy.
11. 64° at 2 PM (8 hours after 6 AM.)
12. 5000 pens should be produced for a cost of \$200.
13. 8 feet by 16 feet; maximum area is 128 square feet.
14. 2 seconds.
15. The rocket reaches its maximum height of 500 feet 10 seconds after lift-off.
16. The hammer reaches a maximum height of approximately 13.62 feet. The hammer is in the air approximately 1.61 seconds.