${MA~123}~{
m Fall~2023}$ Elementary Calculus

Exam 1

09/21/23

Name:			

Student ID #: 9_____ Sec: ____

Do not remove this answer page — you will turn in the entire exam. You have two hours to do this exam. No books or notes may be used. You may use an ACT-approved calculator during the exam, but NO calculator with a Computer Algebra System (CAS), networking, or camera is permitted. Absolutely no cell phone use during the exam is allowed.

The exam consists of 2 short answer questions and 18 multiple choice questions. Answer the short answer questions on the back of this page, and record your answers to the multiple choice questions on this page. For each multiple choice question, you will need to fill in the circle corresponding to the correct answer. For example, if (a) is correct, you must shade

(a) (b) (c) (d) (e)

It is your responsibility to make it CLEAR which response has been chosen. You will not get credit unless the correct answer has been clearly marked on this page.

GOOD LUCK!

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3. ($\mathbf{a})$ ((\mathbf{b}) ((\mathbf{c})	(\mathbf{d})	(\mathbf{e})	12.	\mathbf{a}) (b) ($[\mathbf{c}]$) (\mathbf{d}) (e

$$5. (a) (b) (c) (d) (e)$$
 $14. (a) (b) (c) (d) (e)$

$$\mathbf{6.} \stackrel{\frown}{\mathbf{a}} \stackrel{\frown}{\mathbf{b}} \stackrel{\frown}{\mathbf{c}} \stackrel{\frown}{\mathbf{d}} \stackrel{\frown}{\mathbf{e}} \qquad \qquad \mathbf{15.} \stackrel{\frown}{\mathbf{a}} \stackrel{\frown}{\mathbf{b}} \stackrel{\frown}{\mathbf{c}} \stackrel{\frown}{\mathbf{d}} \stackrel{\frown}{\mathbf{e}}$$

$$7. (a) (b) (c) (d) (e) 16. (a) (b) (c) (d) (e)$$

$$\mathbf{8.} \stackrel{\frown}{\mathbf{a}} \stackrel{\frown}{\mathbf{b}} \stackrel{\frown}{\mathbf{c}} \stackrel{\frown}{\mathbf{d}} \stackrel{\frown}{\mathbf{e}} \qquad \qquad \mathbf{17.} \stackrel{\frown}{\mathbf{a}} \stackrel{\frown}{\mathbf{b}} \stackrel{\frown}{\mathbf{c}} \stackrel{\frown}{\mathbf{d}} \stackrel{\frown}{\mathbf{e}}$$

$$9. (a) (b) (c) (d) (e)$$
 $18. (a) (b) (c) (d) (e)$

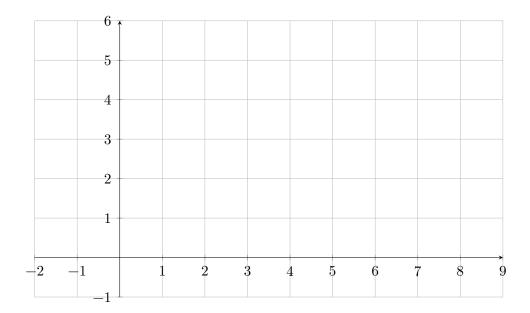
$$10. (a) (b) (c) (d) (e) 19. (a) (b) (c) (d) (e)$$

$$11. (a) (b) (c) (d) (e) 20. (a) (b) (c) (d) (e)$$

Short Answer Questions

Each question is an opportunity to earn 5 points. Points are earned on the clarity and correctness of your work, not merely on having a correct answer somewhere.

1. Sketch the graph of a function y = f(x) which satisfies the following properties: $\lim_{x \to 1^-} f(x) = 4$, $\lim_{x \to 1^+} f(x) = 2$, f(1) = 0, $\lim_{x \to 5} f(x) = 3$, and f(x) is continuous for all x except x = 1.



2. Let $g(x) = x^2 - 3x + 8$. Determine a value of c between x = 4 and x = 9 such that the average rate of change of g(x) from x = 4 to x = 9 is equal to the instantaneous rate of change at x = c.

Name:	
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Multiple Choice Questions

Clearly mark your answer on the cover page on this exam for credit.

3. A train traveled from city A to city B then traveled from city B to city C. The train left city A at 10:00am and arrived at city B at 12:30pm. The train left city B at 3:00pm and arrived at city C at 5:00pm. The average speed of the train, while traveling from A to B, was 57 miles per hour. The average speed of the train, while traveling from B to C, was 21 miles per hour. What was the average speed of the train from city A to city C, including the 2.5 hour wait at city B?

Possibilities:

- (a) 78 miles per hour
- (b) $\frac{369}{14}$ miles per hour
- (c) $\frac{351}{14}$ miles per hour
- (d) 39 miles per hour
- (e) 41 miles per hour
- 4. For the function $f(x) = x^2 + 2x + 9$, determine the equation of the tangent line to the graph of y = f(x) at x = 5.

(a)
$$y = 44x - 208$$

(b)
$$y = \frac{32}{5}x + 12$$

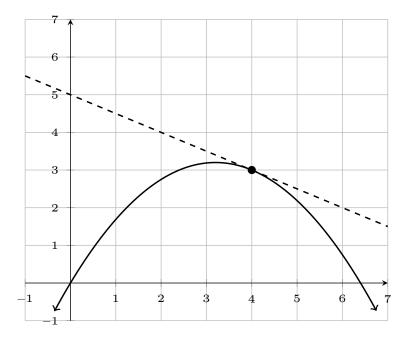
(c)
$$y = 12x - 16$$

(d)
$$y = 2x^2 - 8x + 34$$

(e)
$$y = 44x + 12$$

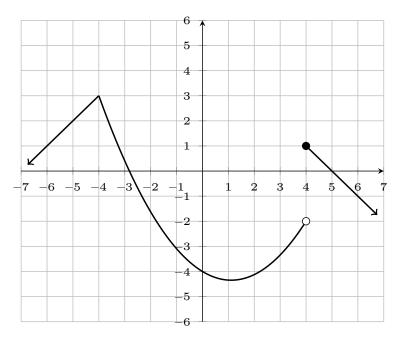
Possibilities:

- (a) $-\frac{1}{2}$
- (b) 2
- (c) -2
- (d) 3
- (e) -1



6. The graph of y = f(x) is shown below. Evaluate $\lim_{x \to 4^-} f(x)$.

- (a) 3
- (b) $-\frac{1}{2}$
- (c) The limit does not exist.
- (d) -2
- (e) 1



7. Let $f(x) = 4x^2 + 5x + 8$. Choose the simplified form of $\frac{f(x+h) - f(x)}{h}$.

Possibilities:

- (a) 1
- (b) 18x + 8h + 21
- (c) 8x + 4h + 5
- (d) 10x + 16
- (e) 8h + 5

8. Consider the function $f(x) = \begin{cases} Ax^2 & \text{if } x < 2, \\ 24 - Ax & \text{if } x \ge 2. \end{cases}$ Determine a value of A such that f(x) is continuous at x = 2.

- (a) 4
- (b) 3
- (c) 2
- (d) 0
- (e) 6

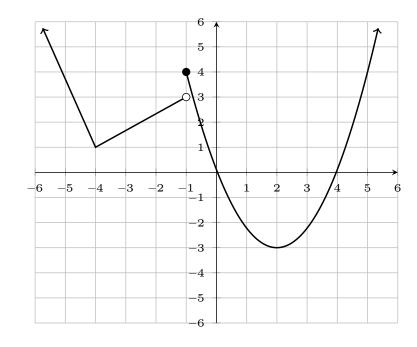
9. Determine all values of x where the derivative of $f(x) = |x^3 + 9x^2|$ is not defined.

Possibilities:

- (a) x = 0 only
- (b) x = -9 and x = 0
- (c) x = -9 only
- (d) x = 0 and x = 9
- (e) x = 9 only

10. The graph of y = f(x) is shown below. The function is continuous, except at which x values?

- (a) -4 and -1
- (b) -1 only
- (c) -4 only
- (d) 3 and 4 only
- (e) 1, 3 and 4



11. Given

$$f(x) = \begin{cases} -5x^2 - 8x - 4 & \text{if } x < -7, \\ 7 + 6x & \text{if } -7 \le x < 3, \\ \sqrt{x^2 + 7} & \text{if } x \ge 3, \end{cases}$$

evaluate $\lim_{x \to 3^+} f(x)$.

Possibilities:

- (a) 25
- (b) -35
- (c) 10
- (d) 4
- (e) -193

12. Evaluate $\lim_{x \to \infty} \frac{5x + 19x^7 + 8}{17 + x^2 + 7x^7}$.

- (a) The limit does not exist.
- (b) $\frac{5}{17}$
- (c) $\frac{19}{7}$
- (d) $\frac{8}{17}$
- (e) $\frac{32}{25}$

13. Let $f(x) = 3x^2$. Determine a value of x such that the average rate of change of f(x) from 5 to x equals 36.

Possibilities:

- (a) 5
- (b) 17
- (c) 10
- (d) 12
- (e) 7

14. Let $f(x) = 3x^2 - 32x + 3$. At what value of x does the tangent line to the graph of y = f(x) have slope 5?

- (a) $-\frac{9}{2}$
- (b) $\frac{16}{3} + \frac{1}{3}\sqrt{262}$
- (c) $\frac{17}{3}$
- $(d) \ \frac{37}{2}$
- (e) $\frac{37}{6}$

15. If h(t) represents the height of an object in feet above ground level at time t seconds and h(t) is given by $h(t) = -16t^2 + 4t + 11$, determine the height of the object at the time when its speed is zero.

Possibilities:

- (a) $\frac{1}{4}$
- (b) $\frac{1}{8}$
- (c) 4
- (d) $\frac{45}{4}$
- (e) 11

16. Find the average rate of change of $f(x) = x^2 - 10x + 8$ from x = 2 to x = 13.

- (a) -10
- (b) 5
- (c) $\frac{593}{13}$
- (d) $\frac{13}{5}$
- (e) -5

17. Evaluate $\lim_{t\to 4} \frac{t^2+t-20}{t^2+4t-32}$.

Possibilities:

- (a) The limit does not exist.
- (b) $\frac{1}{4}$
- (c) 0
- (d) 1
- (e) $\frac{3}{4}$

18. Let $f(x) = 8x^2 - 5x + 7$. Determine the instantaneous rate of change of f(x) at x = 2.

- (a) 27
- (b) $\frac{7}{16}$
- (c) 29
- (d) 34
- (e) 32

19. Suppose $\lim_{x\to 6} f(x) = 7$ and $\lim_{x\to 6} g(x) = -3$. Evaluate $\lim_{x\to 6} \left((x+5)f(x) + \frac{x+2}{g(x)} \right)$.

Possibilities:

- (a) $-\frac{157}{7}$
- (b) $-\frac{223}{7}$
- (c) $\frac{157}{3}$
- (d) $\frac{223}{3}$
- (e) $\frac{239}{3}$

20. The graph of y = f(x) is shown below. Compute the average rate of change of f(x) from x = -5 to x = 3.

- (a) $-\frac{5}{8}$
- (b) $-\frac{3}{2}$
- (c) $\frac{5}{8}$
- (d) $-\frac{8}{5}$
- (e) $-\frac{2}{3}$

