MA 213 — Calculus III
 Fall 2016

 Exam 3
 November 16, 2016

Name: \_\_\_\_\_

Section: \_\_\_\_\_

Last 4 digits of student ID #: \_\_\_\_\_

- No books or notes may be used.
- Turn off all your electronic devices and do not wear ear-plugs during the exam.
- You may use a calculator, but not one which has symbolic manipulation capabilities or a QWERTY keyboard.
- Additional blank sheets for scratch work are available upon request.
- Multiple Choice Questions: Record your answers on the right of this cover page by marking the box corresponding to the correct answer.
- Free Response Questions: Show all your work on the page of the problem. Clearly indicate your answer and the reasoning used to arrive at that answer.

## Multiple Choice Answers

Question					
1	А	В	С	D	Е
2	А	В	С	D	Е
3	А	В	С	D	Е
4	А	В	С	D	Е
5	А	В	С	D	Е

## Exam Scores

Question	Score	Total
MC		30
6		10
7		10
8		10
9		10
10		10
11		10
12		10
Total		100

# Unsupported answers for the free response questions may not receive credit!

#### Record the correct answer to the following problems on the front page of this exam.

- 1. (6 points) A point in space has rectangular coordinates  $(-1, -\sqrt{3}, 2\sqrt{3})$ . Find its spherical coordinates  $(\rho, \theta, \phi)$ .
  - A.  $\rho = 4, \ \theta = \pi/6, \ \phi = \pi/3.$
  - B.  $\rho = 4, \ \theta = \pi/3, \ \phi = \pi/6.$
  - C.  $\rho = 4, \ \theta = 4\pi/3, \ \phi = \pi/6.$
  - D.  $\rho = 4, \ \theta = 2\pi/3, \ \phi = -\pi/6.$
  - E.  $\rho = 4, \ \theta = 2\pi/3, \ \phi = \pi/6.$

- 2. (6 points) Find the cylindrical coordinates of a point whose rectangular coordinates are (1, -1, -1).
  - A.  $(\sqrt{2}, 5\pi/4, -1).$
  - B.  $(\sqrt{3}, 5\pi/4, -1).$
  - C.  $(\sqrt{2}, 3\pi/4, -1).$
  - D.  $(\sqrt{3}, 7\pi/4, -1).$
  - E.  $(\sqrt{2}, 7\pi/4, -1).$

## Record the correct answer to the following problems on the front page of this exam.

**3.** (6 points) Let *E* be the solid above the cone  $z = \sqrt{x^2 + y^2}$  and below the sphere  $x^2 + y^2 + z^2 = z$ . Which of the following iterated integrals evaluates

$$\iiint_E f(x,y,z) \, dV$$

in spherical coordinates?

A.  

$$\int_{0}^{\pi/2} \int_{0}^{2\pi} \int_{0}^{\cos\phi} f(\rho \sin\phi \cos\theta, \rho \sin\phi \sin\theta, \rho \cos\phi) \rho^{2} \sin\phi \, d\rho \, d\theta \, d\phi.$$

В.

$$\int_0^{\pi/4} \int_0^{2\pi} \int_0^{\sin\phi} f(\rho \sin\phi \cos\theta, \rho \sin\phi \sin\theta, \rho \cos\phi) \rho^2 \sin\phi \, d\rho \, d\theta \, d\phi.$$

$$\int_0^{\pi/2} \int_0^{2\pi} \int_0^{\sin\phi} f(\rho\sin\phi\cos\theta, \rho\sin\phi\sin\theta, \rho\cos\phi) \rho^2 \sin\phi \, d\rho \, d\theta \, d\phi.$$

D.

С.

$$\int_0^{\pi/4} \int_0^{2\pi} \int_0^{\cos\phi} f(\rho\sin\phi\cos\theta, \rho\sin\phi\sin\theta, \rho\cos\phi) \rho^2 \sin\phi \, d\rho \, d\theta \, d\phi.$$

Е.

$$\int_0^{\pi/2} \int_0^{2\pi} \int_0^{\cos\phi} f(\rho \sin\phi \cos\theta, \rho \sin\phi \sin\theta, \rho \sin\phi) \rho^2 \cos\phi \, d\rho \, d\theta \, d\phi.$$

### Record the correct answer to the following problems on the front page of this exam.

- 4. (6 points) The area of the part of the plane 2x+2y+z = 1 inside the cylinder  $x^2+y^2 \le 9$  is
  - A.  $\pi$
  - B.  $3\pi$
  - C.  $9\pi$
  - D.  $27\pi$
  - E. none of the above

- 5. (6 points) The spherical coordinates  $(\rho, \theta, \phi)$  of a point in space are  $(1, \pi/3, \pi/6)$ . Then the cylindrical coordinates of the point are:
  - A.  $(1/2, \pi/3, \sqrt{3}/4)$
  - B.  $(\sqrt{3}/2, \pi/3, \pi/6)$
  - C.  $(\sqrt{3}/2, \pi/6, \pi/6)$
  - D.  $(\sqrt{2}/2, \pi/3, \sqrt{6}/4)$
  - E.  $(1/2, \pi/3, \sqrt{3}/2)$

6. (10 points) Find the area of the region inside the circle  $r = 3\cos\theta$  and outside the cardioid  $r = 1 + \cos\theta$ .

7. (10 points) Use triple integrals to find the volume of the tetrahedron bounded by the planes x = y, y = 1, z = 0, and x - 2y + z = 0.

8. (10 points) Find the moment of inertia  $I_y$  of a lamina shaped as the circular sector  $E = \{(x, y) \mid x \ge 0, y \ge 0, x^2 + y^2 \le 4\}$ , if the density at (x, y) is  $\rho(x, y) = y$ .

9. (10 points) Find the average value of the function  $f(x, y) = \sqrt{x^2 + y^2}$  over the plane region between the circles  $x^2 + y^2 \le 1$  and  $x^2 + y^2 \le 4$ .

10. (10 points) Change the order of integration in

$$\int_{-1}^{1} \int_{0}^{1-x^2} f(x,y) \, dy \, dx.$$

**11.** (10 points) Evaluate

$$\iint_E \frac{e^y}{y} \, dA,$$

where E is the triangle bounded by the lines y = x, y = 2x, and y = 2.

12. (10 points) Use geometry and symmetry to evaluate

$$\iint_E \left(3 + \sin(y^3)\right) dA,$$

where E is the disk  $\{(x, y) \mid x^2 + y^2 \le 4\}$ . [Be sure to justify your answer.]