

Name: _____

Section: _____

Last 4 digits of student ID #: _____

- No books or notes may be used.
- Turn off all your electronic devices and do not wear ear-plugs during the exam.
- You may use a calculator, but not one which has symbolic manipulation capabilities or a QWERTY keyboard.
- Additional blank sheets for scratch work are available upon request.
- All questions are free response questions. Show all your work on the page of the problem. Clearly indicate your answer and the reasoning used to arrive at that answer. Unsupported answers may not receive credit.

Exam Scores

*Do not write in
the table below*

Question	Score	Total
1		10
2		10
3		10
4		10
5		10
6		10
7		10
8		10
9		10
10		10
Total		100

Free Response. Always show your work!

1. (10 points) Change the order of integration in the following iterated integral:

$$\int_0^1 \int_{\sqrt{x}}^1 e^{x^3 y} dy dx.$$

Do not evaluate the integral.

2. (10 points) Find the average value of $f(x, y) = xy$ over the triangle with vertices $(0, 0)$, $(1, 0)$, and $(1, 3)$.

Free Response. Always show your work!

- 3.** (10 points) Use polar coordinates to find the volume of the solid E inside the cylinder $x^2 + y^2 = 1$ and the ellipsoid $4x^2 + 4y^2 + z^2 = 64$, and above the xy -plane.

Free Response. Always show your work!

4. (10 points) A lamina occupies the part of the disk $x^2 + y^2 \leq 1$ in the first quadrant. Find its center of mass, if the density is given by $\rho(x, y) = x + y$.

Note: You may need to use the formulas

$$\sin^2 \alpha = \frac{1 - \cos(2\alpha)}{2}, \quad \cos^2 \alpha = \frac{1 + \cos(2\alpha)}{2}.$$

Free Response. Always show your work!

5. (10 points) Find the surface area of the part of the plane $6x + 4y + 2z = 1$ that lies inside the cylinder $x^2 + y^2 = 25$.

6. (10 points) Evaluate

$$\int_0^2 \int_0^{z^2} \int_0^{y-z} (2x - y) \, dx \, dy \, dz.$$

Free Response. Always show your work!

7. (10 points) Compute the volume of the solid bounded by the paraboloid $z = 4x^2 + 4y^2$ and the plane $z = a$ ($a > 0$).

Free Response. Always show your work!

8. (10 points) Find the spherical coordinates (ρ, θ, ϕ) of the point P whose rectangular coordinates are $(-1, 1, -\sqrt{2})$.
9. (10 points) In spherical coordinates, the equation $\rho = 2 \sin \phi \sin \theta$ represents a sphere. Find the center C and the radius R of this sphere.

Free Response. Always show your work!

10. (10 points) (a) Describe in spherical coordinates the region E that lies between the spheres $x^2 + y^2 + z^2 = 4$ and $x^2 + y^2 + z^2 = 9$.

(b) Express $x^2 + y^2$ in spherical coordinates (ρ, θ, ϕ) .

(c) Write the triple integral

$$\iiint_E (x^2 + y^2) dV$$

as an iterated integral using spherical coordinates. Do not evaluate the integral.