

MA 213 Worksheet #6

Section 12.6 - 13.1

1/29/19

- 1 12.6.1 (a) What does the equation $y = x^2$ represent as a curve in \mathbb{R}^2 .
(b) What does it represent as a surface in \mathbb{R}^3
(c) What does the equation $z = y^2$ represent?

- 2 12.6.7 Describe and sketch the surface $xy = 1$.

- 3 12.6.11 Use traces to sketch and identify the surface $x = y^2 + 4z^2$.

- 4 Reduce the equation to one of the standard forms, classify the surface, and sketch it.
12.6.35 $x^2 + y^2 - 2x - 6y - z + 10 = 0$
12.6.37 $x^2 - y^2 + z^2 - 4x - 2z = 0$.

- 5 12.6.43 Sketch the region bounded by the surfaces $z = \sqrt{x^2 + y^2}$ and $x^2 + y^2 = 1$ for $1 \leq z \leq 2$.

- 6 13.1.7 Sketch the curve $\mathbf{r}(t) = \langle \sin t, t \rangle$. Indicate with an arrow the direction in which t increases.

- 7 13.1.17 Find a vector equation and parametric equations for the line segment that joins $P(2, 0, 0)$ to $Q(6, 2, -2)$.

- 8 13.1.49 Suppose the trajectories of two particles are given by the vector functions
$$\mathbf{r}_1(t) = \langle t^2, 7t - 12, t^2 \rangle \quad \mathbf{r}_2(t) = \langle 4t - 3, t^2, 5t - 6 \rangle$$
for $t \geq 0$. Do the particles collide?

- 9 12.6.21-28 (On back)

21–28 Match the equation with its graph (labeled I–VIII). Give reasons for your choice.

21. $x^2 + 4y^2 + 9z^2 = 1$

22. $9x^2 + 4y^2 + z^2 = 1$

23. $x^2 - y^2 + z^2 = 1$

24. $-x^2 + y^2 - z^2 = 1$

25. $y = 2x^2 + z^2$

26. $y^2 = x^2 + 2z^2$

27. $x^2 + 2z^2 = 1$

28. $y = x^2 - z^2$

