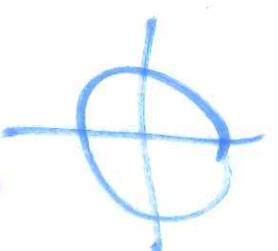


L 41 - M/ 21/ 16.

Monday 12 Dec.

Final.

- Review old tests
- HW 42 (Review).



2. Graph γ * functions

$$\gamma = \pm \sqrt{1-x^2}$$

3. Parametric curve.

$$(\cos(t), \sin(t)), 0 \leq t \leq 2\pi.$$

Describing plane curves.

Plane curve.

1. $x^2 + y^2 = 1$. The unit circle is the collection

of points (x, y) s.t.

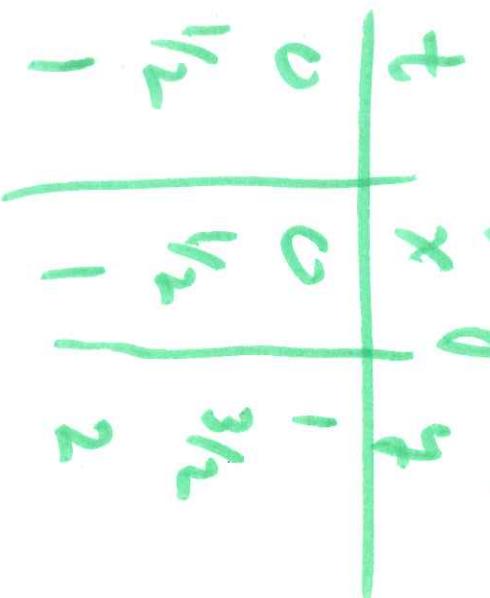
$x^2 + y^2 = 1$.

- Implicit representation. $a \leq t \leq b$.

Example.

$$x(t) = t, \quad y(t) = t^2$$

$$\underline{x(t)} = t^2, \quad \underline{y(t)} = t^3$$

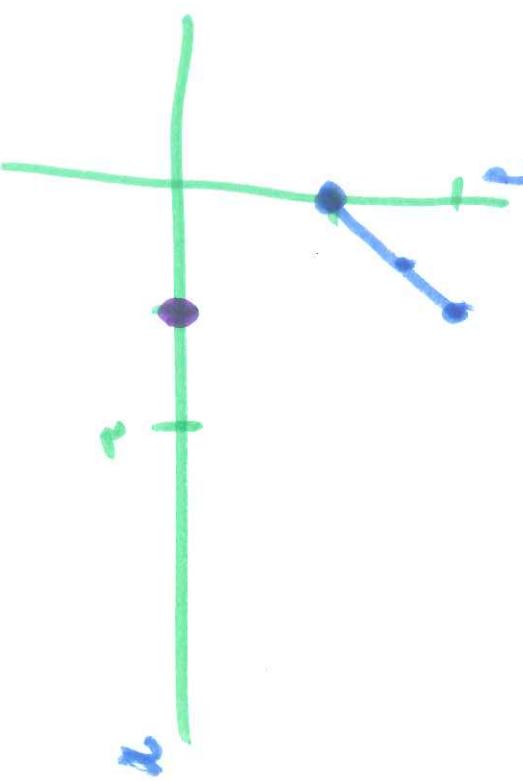


Find an equation in x, y which contains the curve.

Eliminating the parameter t .

$$x = t, \quad y = t^2$$

Chose one equation to solve for t . (Picture easier.)



$$t = \underline{x-1}$$

Substitute to express
y in terms of t into
the other equation

$$y = t^2 + 3t$$

$$= (x-1)^2 + 3(x-1)$$

$$= x^2 - 2x + 1 + 3x - 3$$

$$= x^2 + x - 2.$$

REF #2.

Eliminate + to find
an equation whose
graph contains the
curve

$$(x, y) = (2t+1, t^2).$$

Solution.

$$2t+1 = x,$$

$$t = \frac{1}{2}(x-1)$$

$$y = t^2 = \left(\frac{1}{2}(x-1)\right)^2$$

$$= \frac{1}{4}(x^2 - 2x + 1).$$

Let $x = t$

Find a parametric
representation of the
line through the

line through
(1, 2) with slope -2.

$$(1, 2) \text{ with slope } -2.$$

Find another -

$$x = 1 + t, y = 2 - 2t.$$

Slope = $\frac{\text{change in } y}{\text{change in } x}$

Definition: line P has slope

solutions

$$\text{try } x = 42t.$$

$$y - 2 = -2(x - 1)$$

$$y = -2x + 2 + 2$$

$$= -2x + 4.$$

$$= -84t + 4$$

solution 2

Circles.

$$x = h + a \cos(\theta)$$

$$y = k + a \sin(\theta)$$

describes the unit circle w/ center (h, k) .

radius $a > 0$.

$$x = a \cos(t),$$

$$y = a \sin(t)$$

describes a circle of radius $a > 0$.

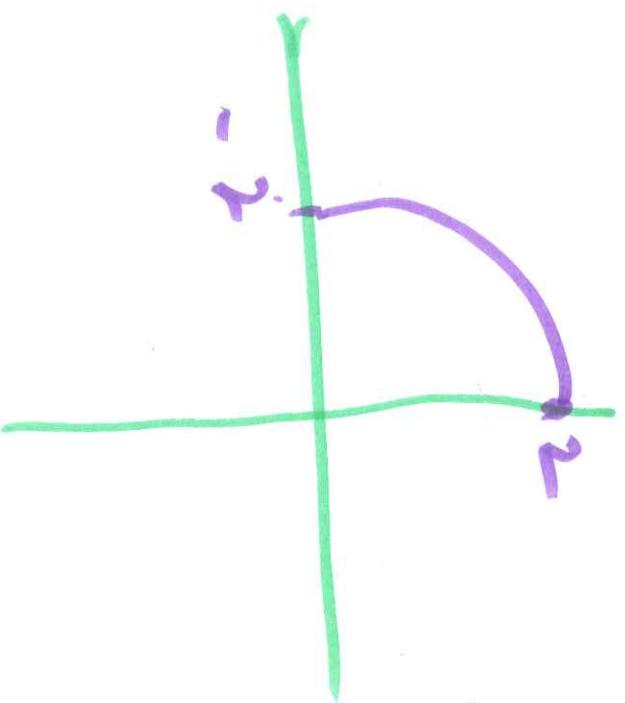
Example. Find a parametric description of the part of the circle of radius 2 center to the line $x + y = 0$ in the first quadrant.

Find a parametric rep.

Circle of half 1 in

ellipse

$$\frac{x^2}{4} + \frac{y^2}{9} = 1.$$



$$x = 2 \cos(t)$$

$$y = 3 \sin(t)$$

$$\frac{(2 \cos(t))^2}{4} + \frac{(3 \sin(t))^2}{9} = 1.$$

$$\frac{\pi}{2} \leq t \leq \pi.$$

$$0 \leq t \leq \pi, \quad y \text{ is zero.}$$

A photon ball travels
along the curve

$$y = 1 + 30.5 \cdot 5 - 5 \cdot (5.5)^2$$

卷之三

$$x(t) = 2e^t$$

$$y(t) = 1 + 30t - 5t^2$$

Will it make it ever

ence 110 m from the

$$-y \not\models y \text{ and } \{ 4, 0 = x \}$$

$$x = 10$$

$$x_0 t = 110 \quad \text{so} \quad t = 5.5 \text{ s.}$$

