MA677 MWF 10-10:50pm CB 345 Fall 2007 Instructor: Russell Brown Office: POT741 Phone: 859 257 3951 russell.brown@uky.edu

The following problems will be due on 31 August.

- 1. Write an iterated integral to compute the area of the triangle $\{(x_1, x_2) : x_1 \ge 0, x_2 \ge 0, x_1 + x_2 \le 1\}.$
- 2. Let S_n be the measure of the simplex $\{(x_1, x_2, \ldots, x_n) : x_j \ge 0, j = 1, \ldots, n \text{ and } \sum_{i=1}^n x_i \le 1\}$. Find S_2 . Give a relation between S_n and S_{n-1} and find S_n .
- 3. (Wheeden and Zygmund, page 97) Let Ω_n be the volume of the unit ball in \mathbb{R}^n . Show that

$$\Omega_n = 2\Omega_{n-1} \int_0^1 (1 - t^2)^{(n-1)/2} dt$$

August 23, 2007