

## Quiz

**Directions:** Carefully read each question below and answer to the best of your ability in the space provided. You **MUST** show your work to receive full credit!

1. (5 points) Find the following indefinite integral:

$$\int \frac{4}{x} + e^x + 3x^2 \, dx.$$

**Solution:**

$$\begin{aligned} \int \frac{4}{x} + e^x + 3x^2 \, dx &= \int \frac{4}{x} \, dx + \int e^x \, dx + \int 3x^2 \, dx \\ &= 4 \ln |x| + e^x + x^3 + C. \end{aligned}$$

2. (5 points) Find the critical numbers of the function

$$g(x) = \frac{6x}{5x^2 + 80}.$$

**Solution:** The problem asks us to find the critical numbers. Remember, critical numbers are the values of  $x$  where  $g'(x) = 0$  or  $g'(x)$  doesn't exist. Thus, we need to take derivative of  $g(x)$  first, that is

$$g'(x) = -\frac{6(x^2 - 16)}{5(x^2 + 16)^2} = -\frac{6(x - 4)(x + 4)}{5(x^2 + 16)^2}.$$

Since  $5(x^2 + 16)^2 > 0$  for any  $x$ , thus we don't have a problem with dividing by 0. Thus,  $g'(x)$  exists everywhere, and we need to find critical point where  $g'(x) = 0$ . Since  $g'(x)$  is a rational function, then it's equal to 0 only when the numerator is equal to 0, that is  $-6(x - 4)(x + 4) = 0$ . Hence  $x = 4$  and  $x = -4$  are the only critical numbers(points).

Name: \_\_\_\_\_

Section (circle one):            021            022            023            024

|           |   |   |       |
|-----------|---|---|-------|
| Question: | 1 | 2 | Total |
| Points:   | 5 | 5 | 10    |
| Score:    |   |   |       |